

Computers Crunching Lipids – From Cell Membranes to Lipoproteins

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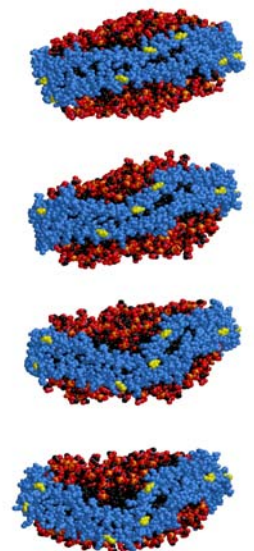
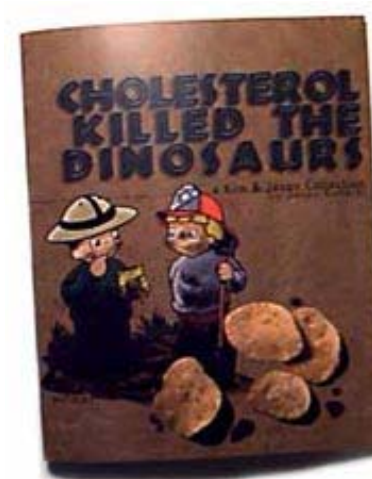
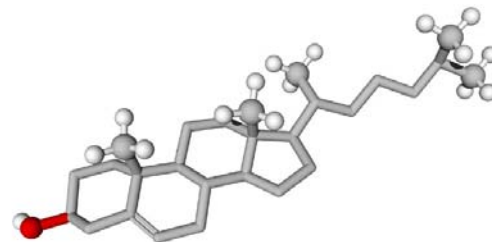
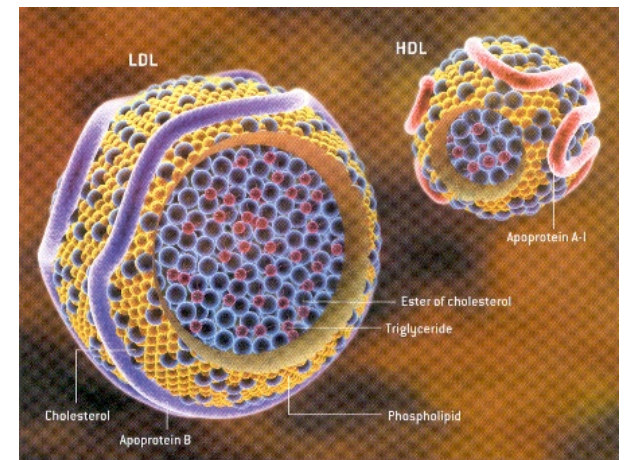
Lab of Physics, Helsinki Univ of Tech

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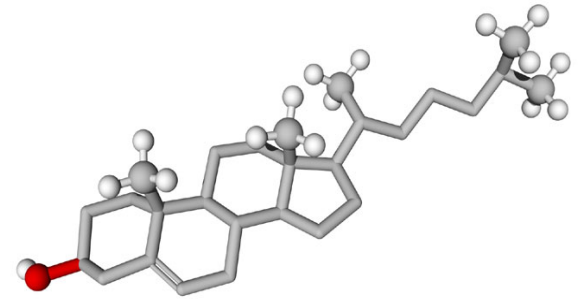
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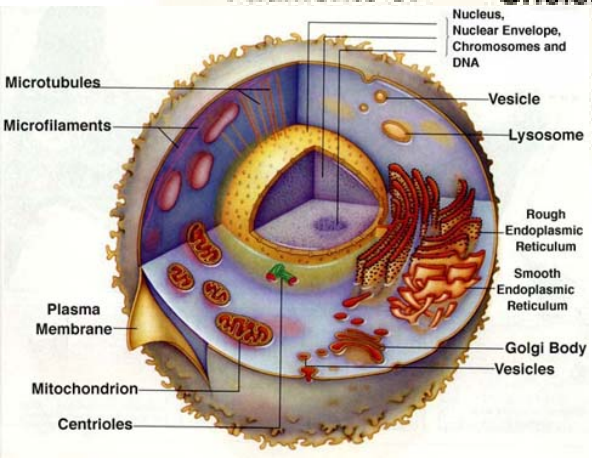
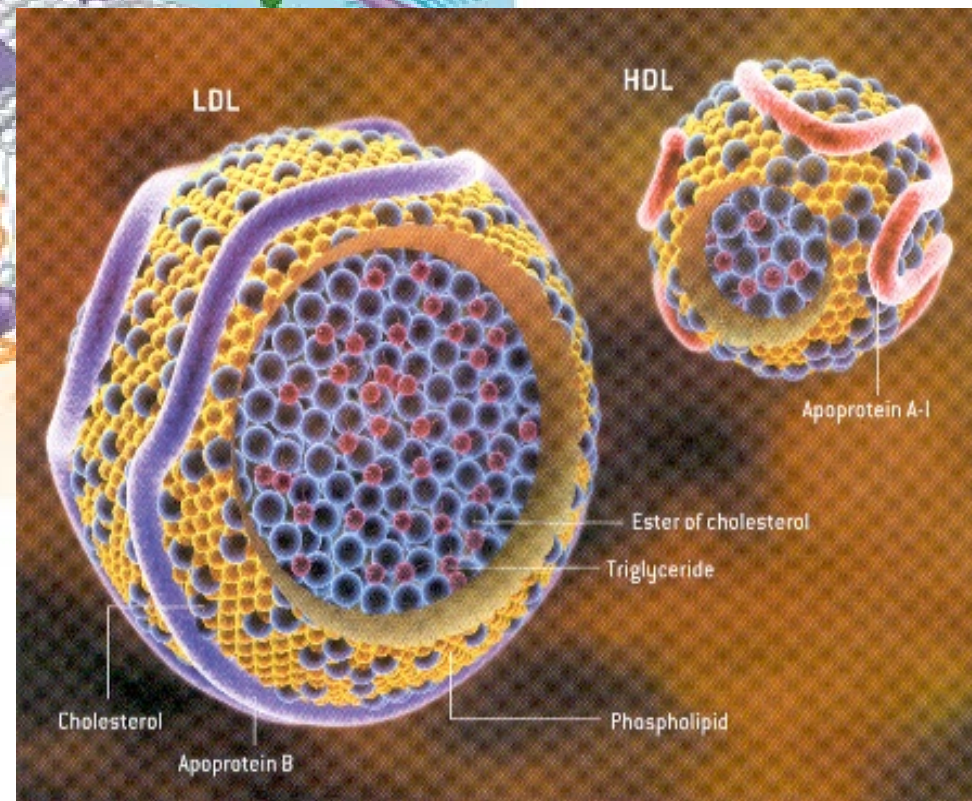
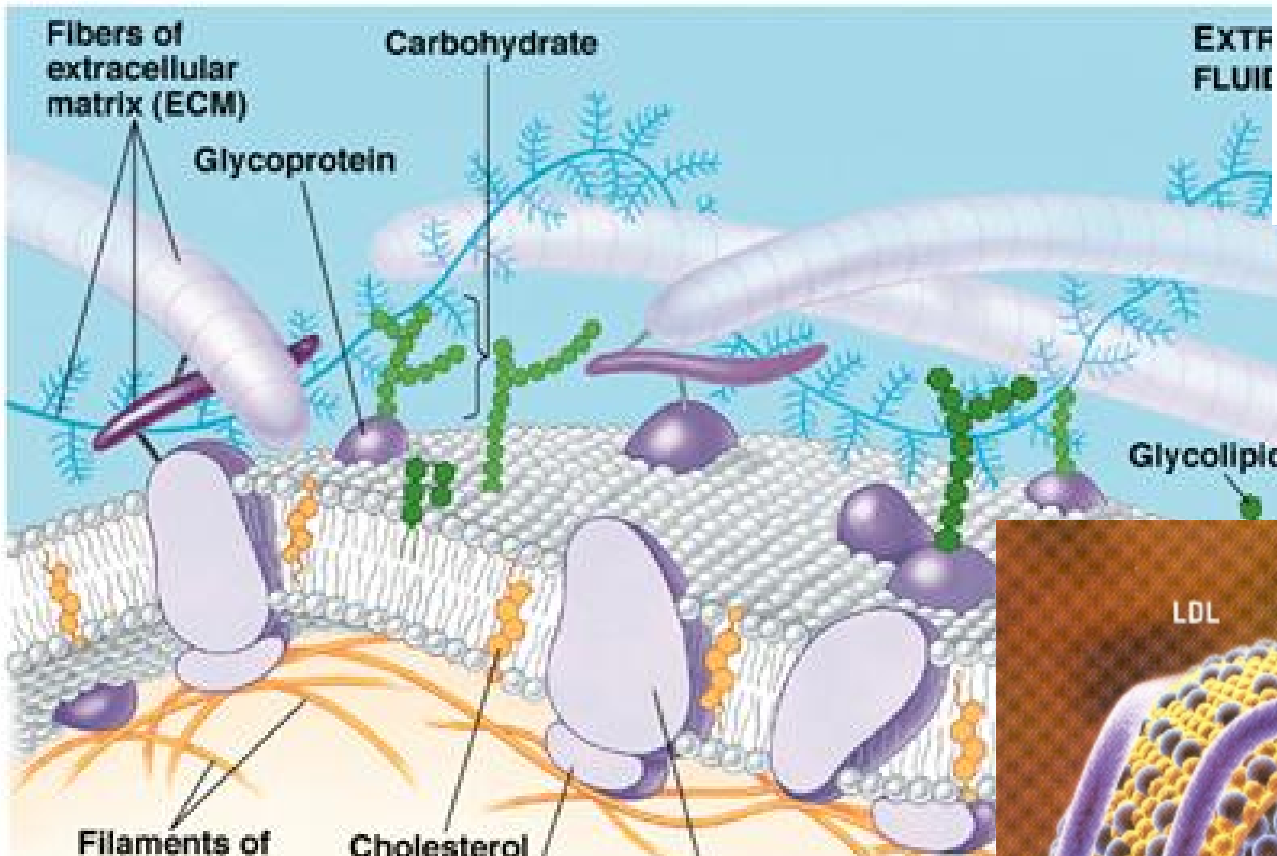
Cray – Helsinki – May 2008



Cholesterol Everywhere



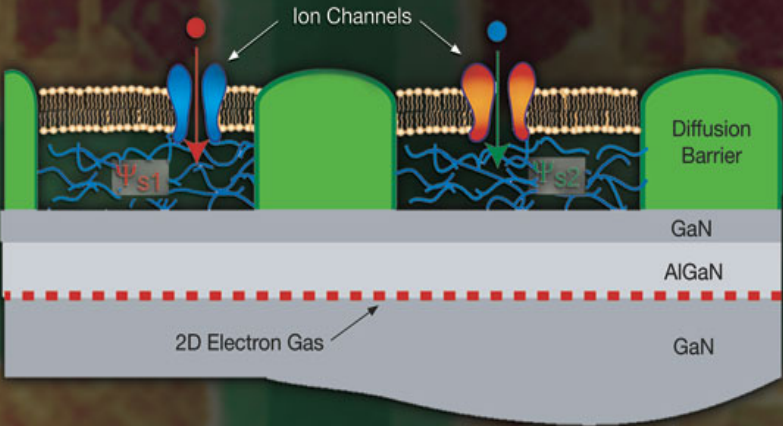
**complexity
& scales !!!**



Membrane Proteins as Biosensors

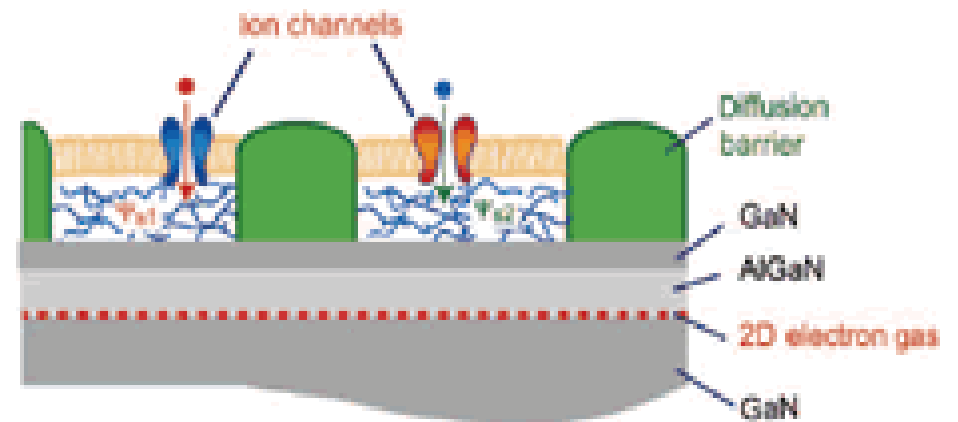
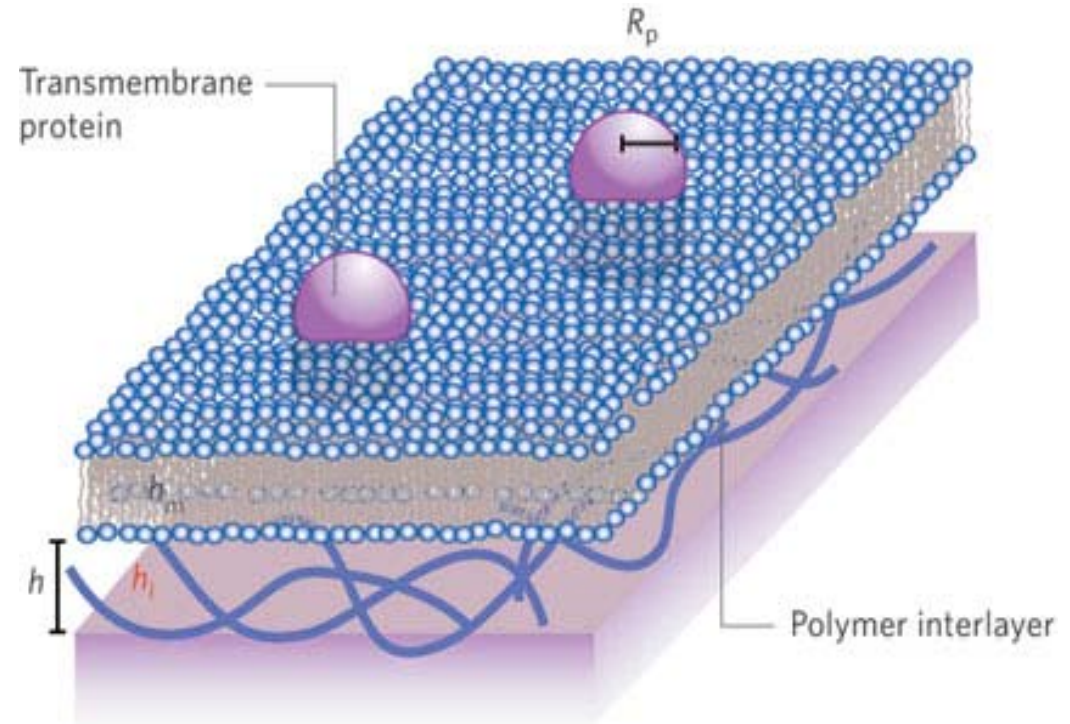

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July 2006, Volume 31, No. 7

Materials Science of Supported Lipid Membranes



Ion Channels
Diffusion Barrier
GaN
AlGaN
2D Electron Gas

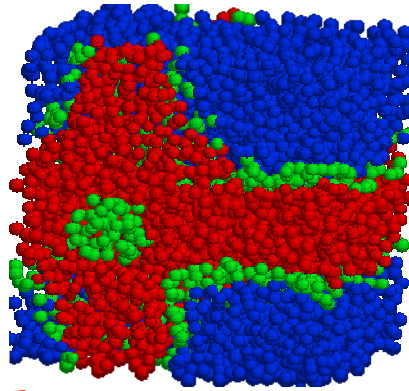
Also in This Issue:
Isotopically Controlled Semiconductors



Multi-scale modeling

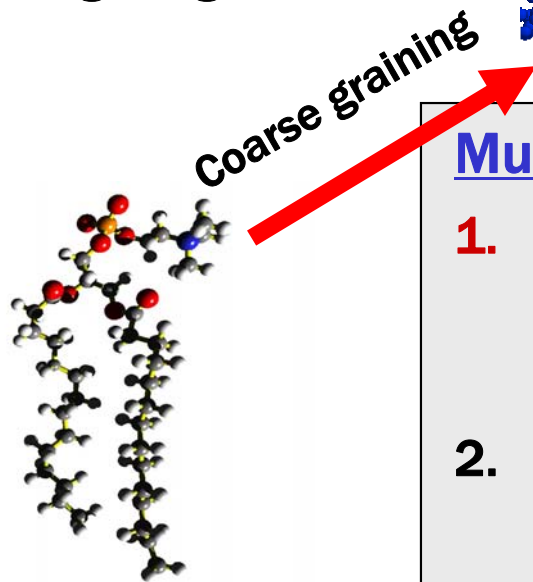
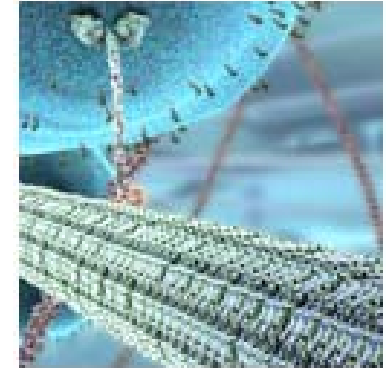
Mesoscale:

- effective interactions
- collective phenomena
- long-range effects



Macroscale:

- times ~ 1 s
- scales $\sim 1\mu$
- large scales



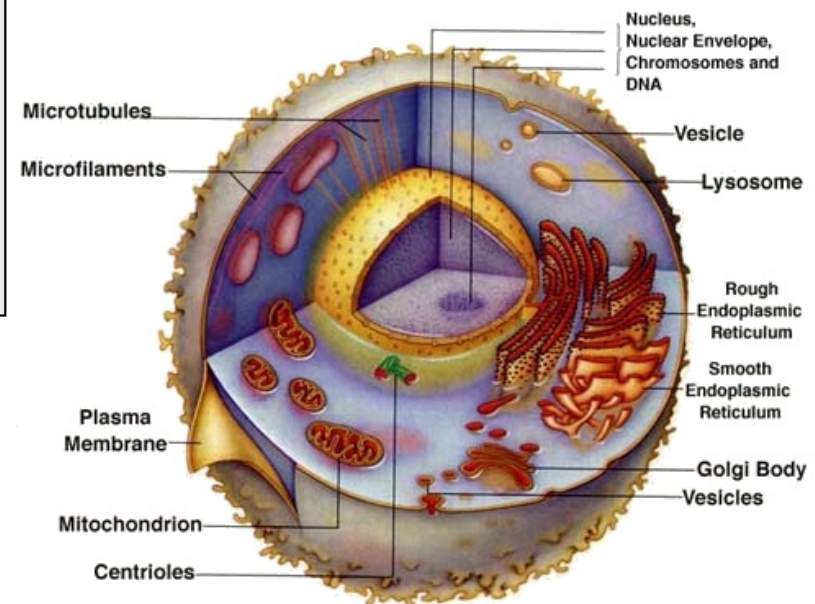
Coarse graining

Multi-scale modeling

1. Development of coarse-graining techniques for molecules and their interactions
2. Bridging atomistic and CG models in applications to actual problems

Atomistic picture:

- microscopic accuracy
- interatomic forces
- intermolecular interactions



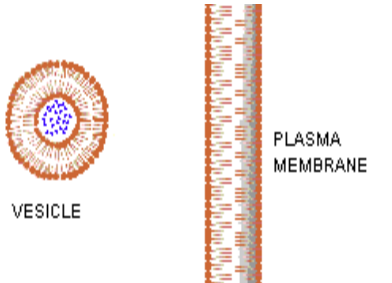
Modeler's toolbox

Various scales, various methods



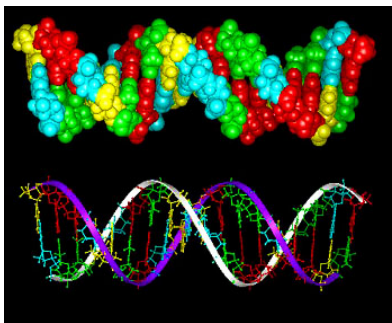
Macroscale:

- times $> 1 \text{ sec}$
- scales $> 1 \mu$
- phase field models, FEM



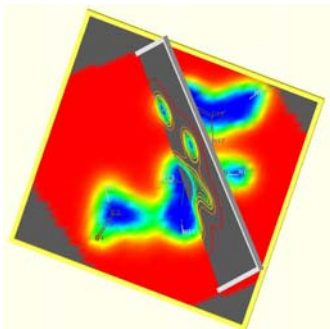
Mesoscale:

- times $\sim 10^{-8} - 10^{-2} \text{ sec}$
- scales $\sim 100 - 10000 \text{ \AA}$
- DPD, coarse graining



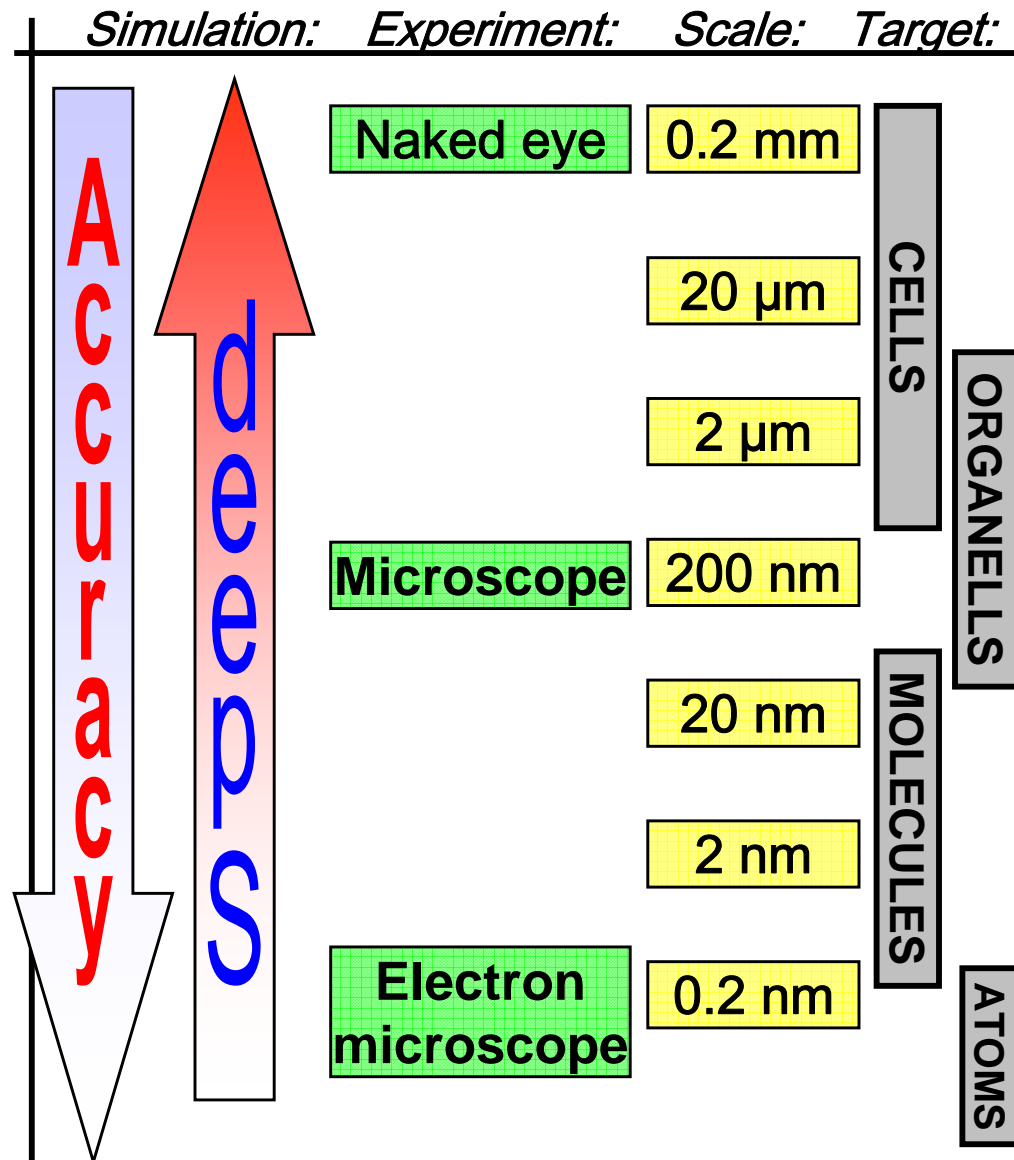
Atomistic scale:

- times $\sim 10^{-15} - 10^{-9} \text{ sec}$
- scales $\sim 1 - 100 \text{ \AA}$
- Classical MD, MC



Subatomistic scale:

- electronic structure
- ab initio
- Green's functions

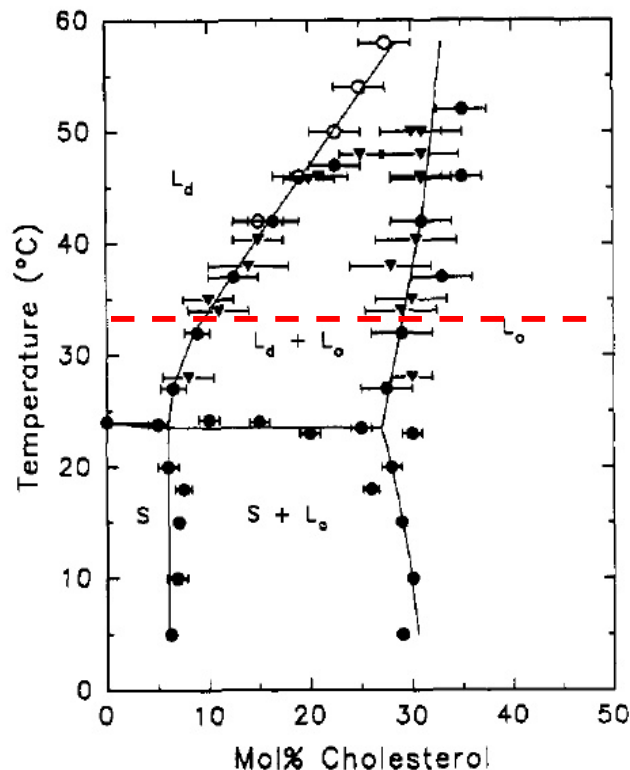


Limits of Atomistic Simulations

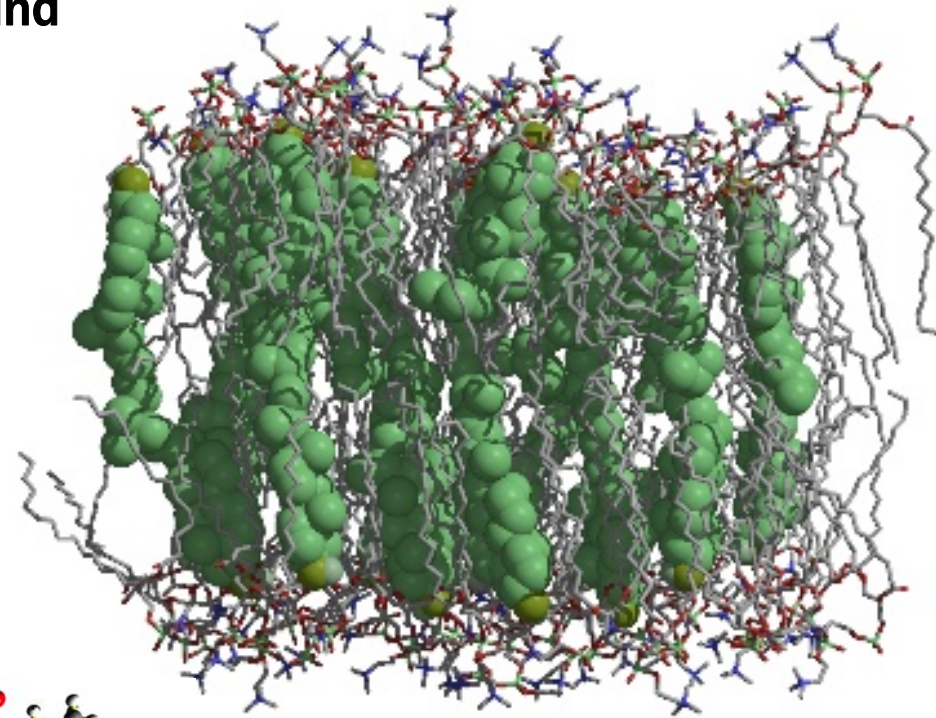
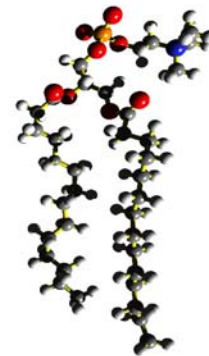
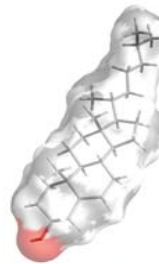
Example for a DPPC/Cholesterol lipid membrane: pros and cons of atomistic simulations for systems of this kind

Classical MD (Gromacs):

- 128 DPPC + Chol molecules + water
- 6 cholesterol concentrations
- Simulated time: 100 ns each



Phase diagram
based on
experiments:
Almeida et al.
(1992)

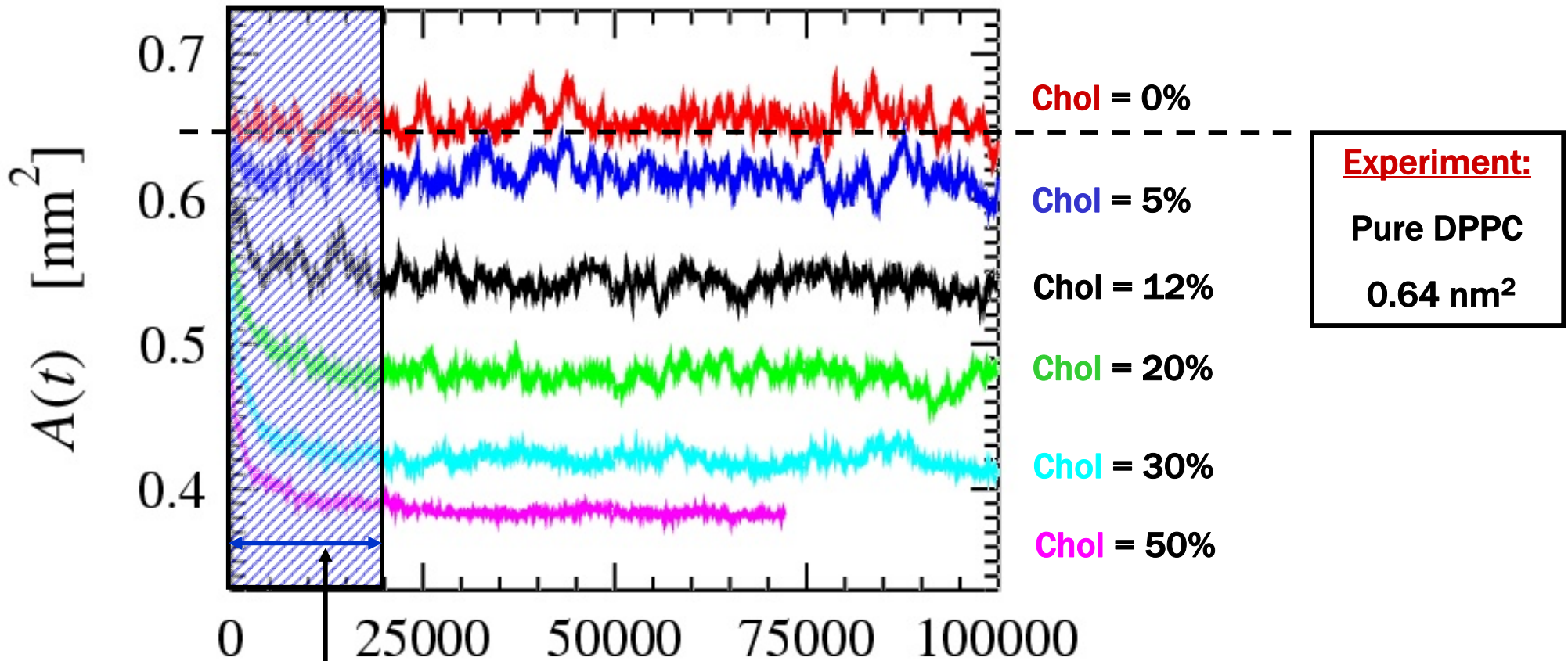


Insight given by atomic-scale modeling in complex biosystems?

[Falck et al., Biophys J 87, 1076 (2004)]

Area per Lipid in Bilayer Plane

DPPC + Cholesterol binary mixture



Equilibration
for 20 ns

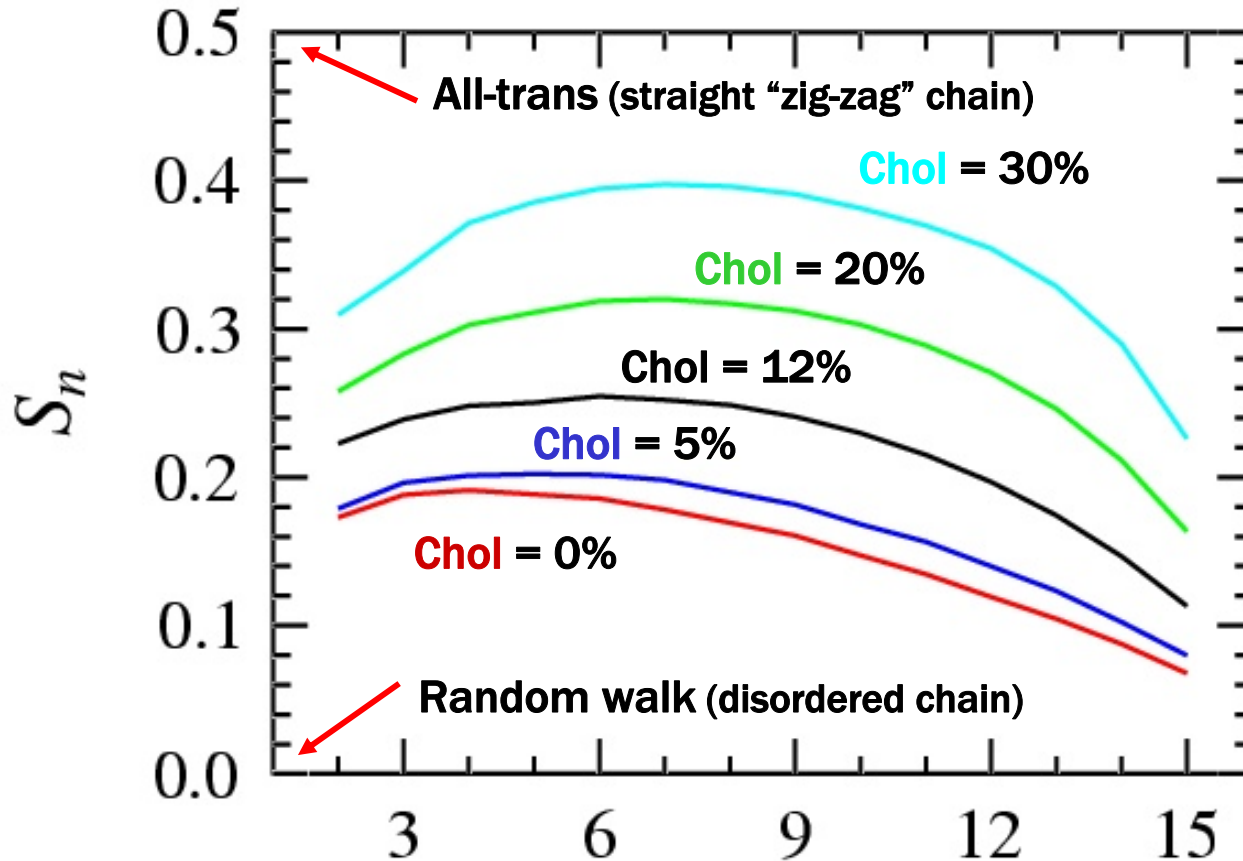
Cholesterol rigidifies the membrane, thus decreasing the area per molecule in agreement with experiments and previous theoretical studies.

[Falck et al., Biophys J 87, 1076 (2004)]

NMR order parameter of acyl chains

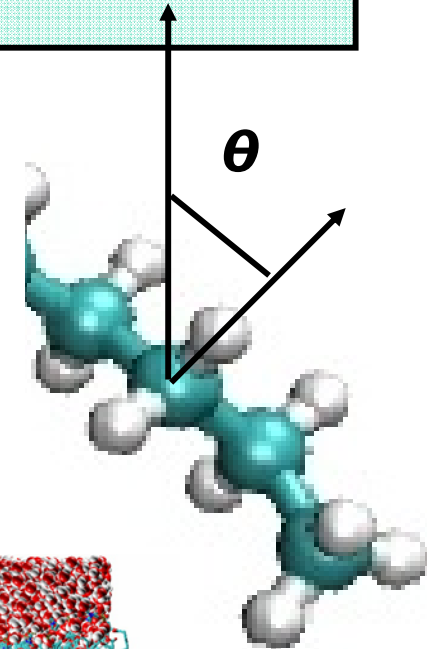
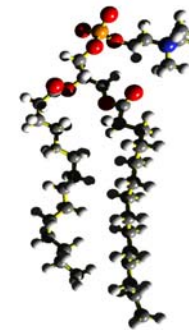
Ordering of lipid acyl chains by cholesterol

Results fully consistent with NMR

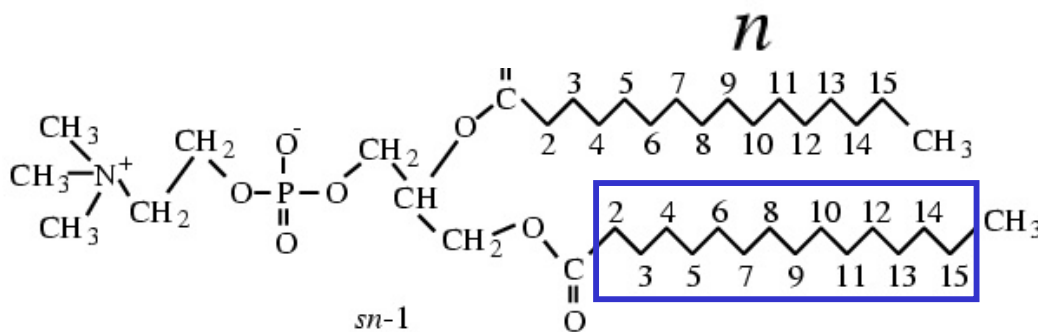
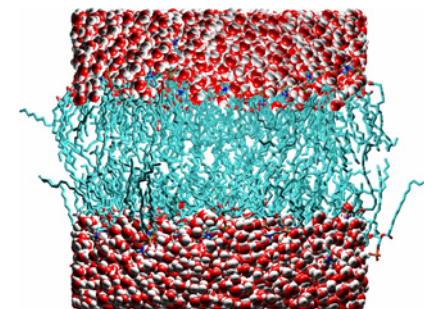


$$S = \frac{3 \langle \cos^2 \theta \rangle - 1}{2}$$

The larger S , the more ordered the chains are.

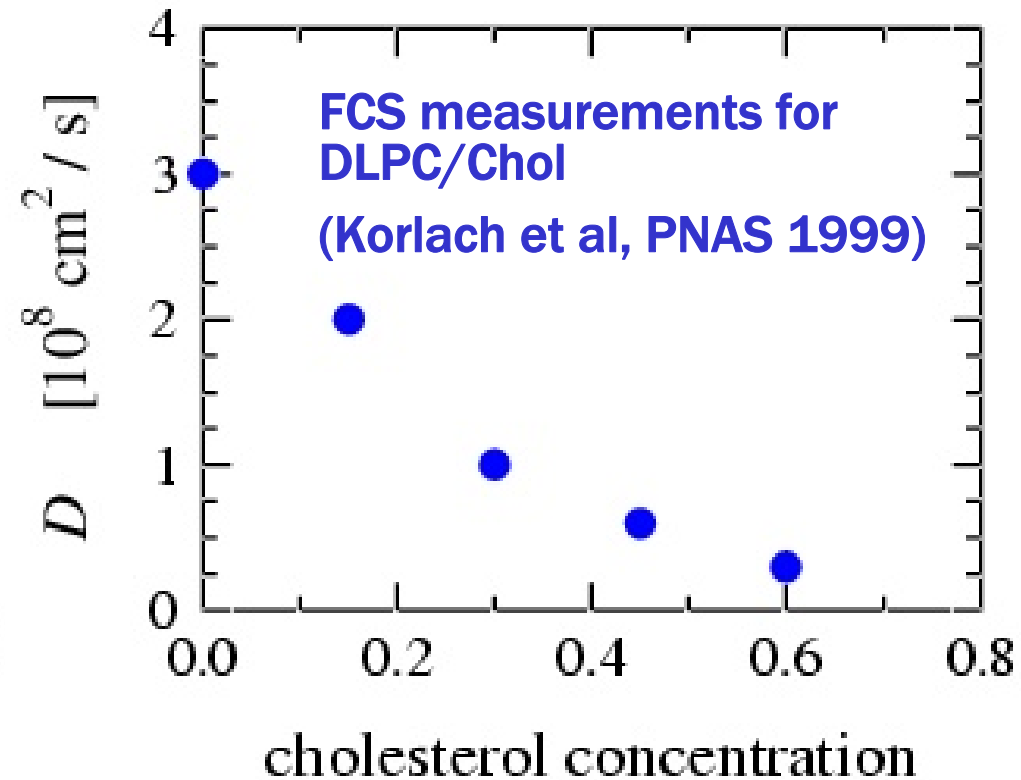
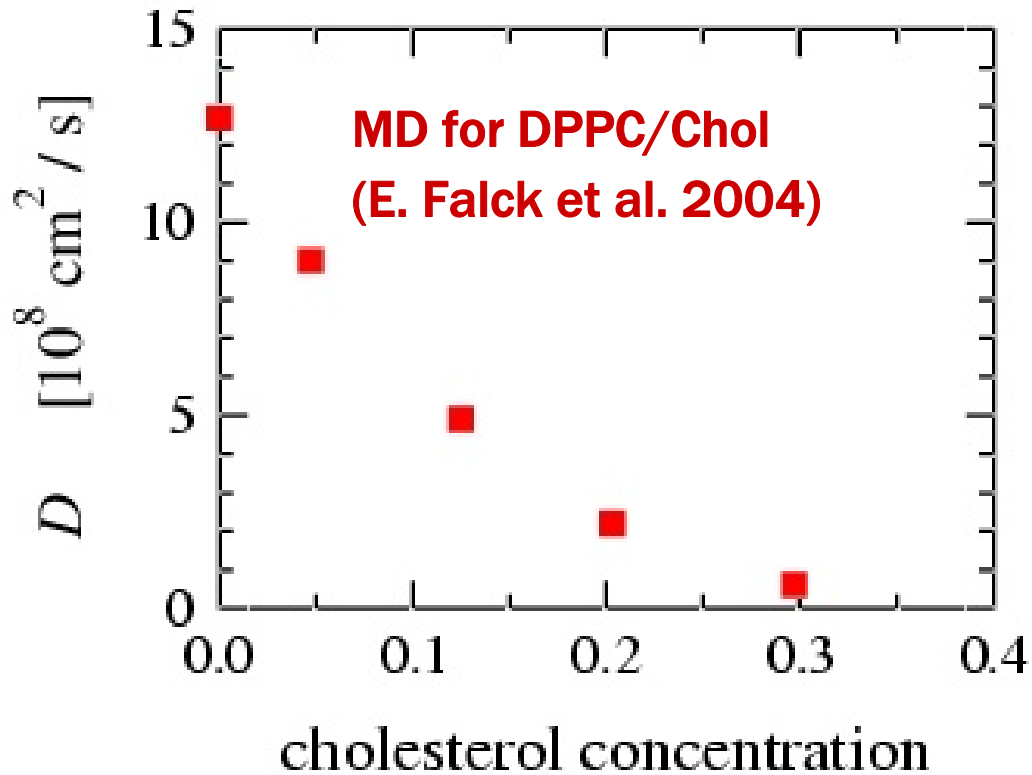


Bilayer normal

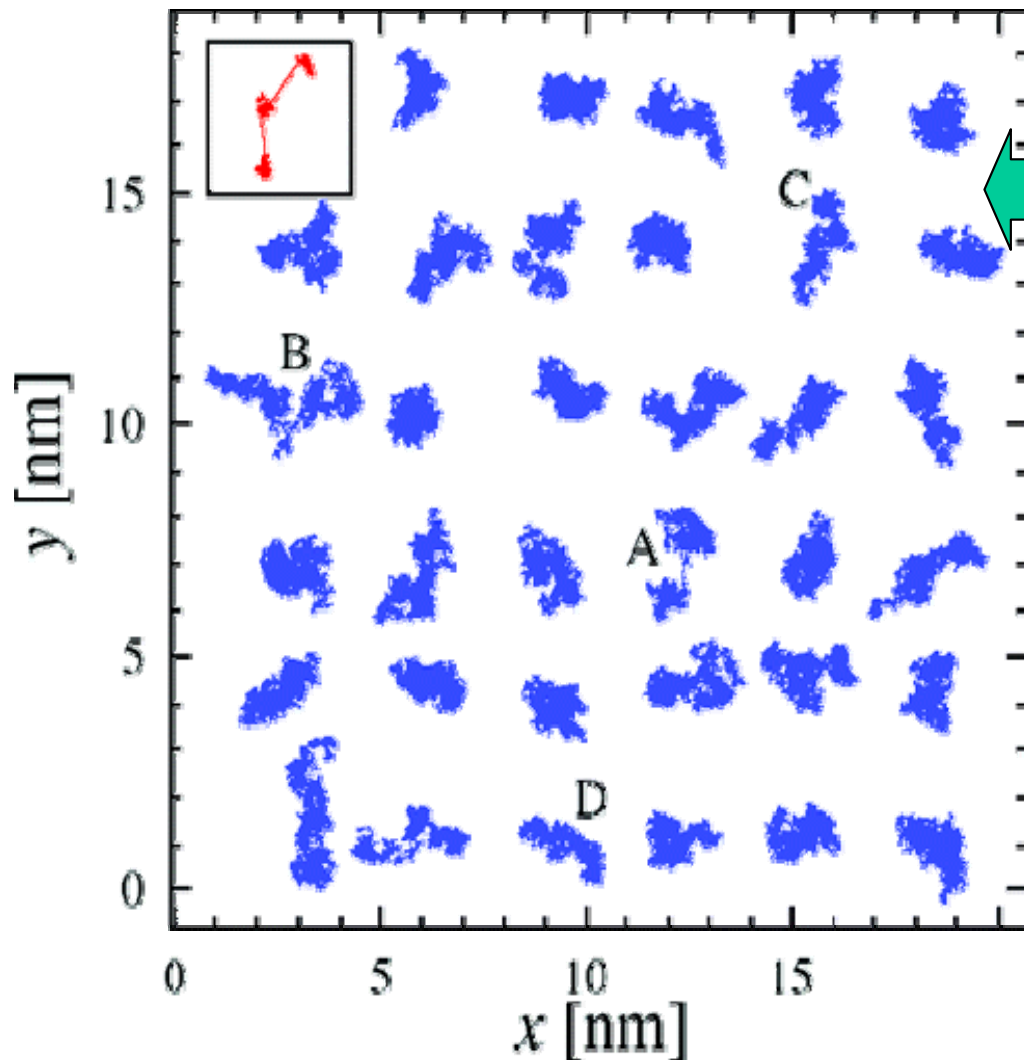


Lateral Diffusion Coefficients

$$D \equiv \lim_{t \rightarrow \infty} \frac{\langle [\vec{r}(t) - \vec{r}(0)]^2 \rangle}{2dt}$$



Lateral Lipid Diffusion Mechanism



Lateral lipid trajectories in a DPPC bilayer of 1152 lipids over a period of 30 ns

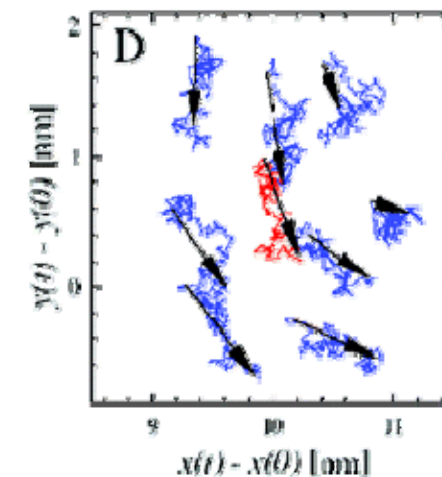
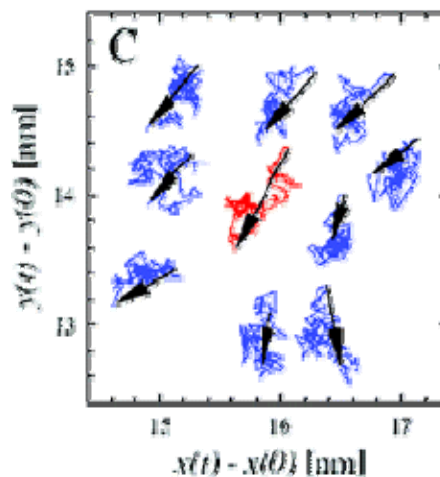
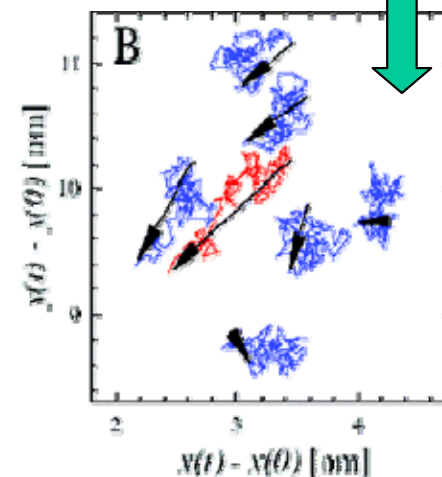
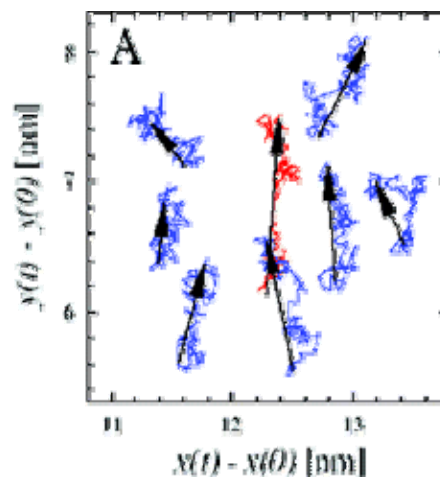
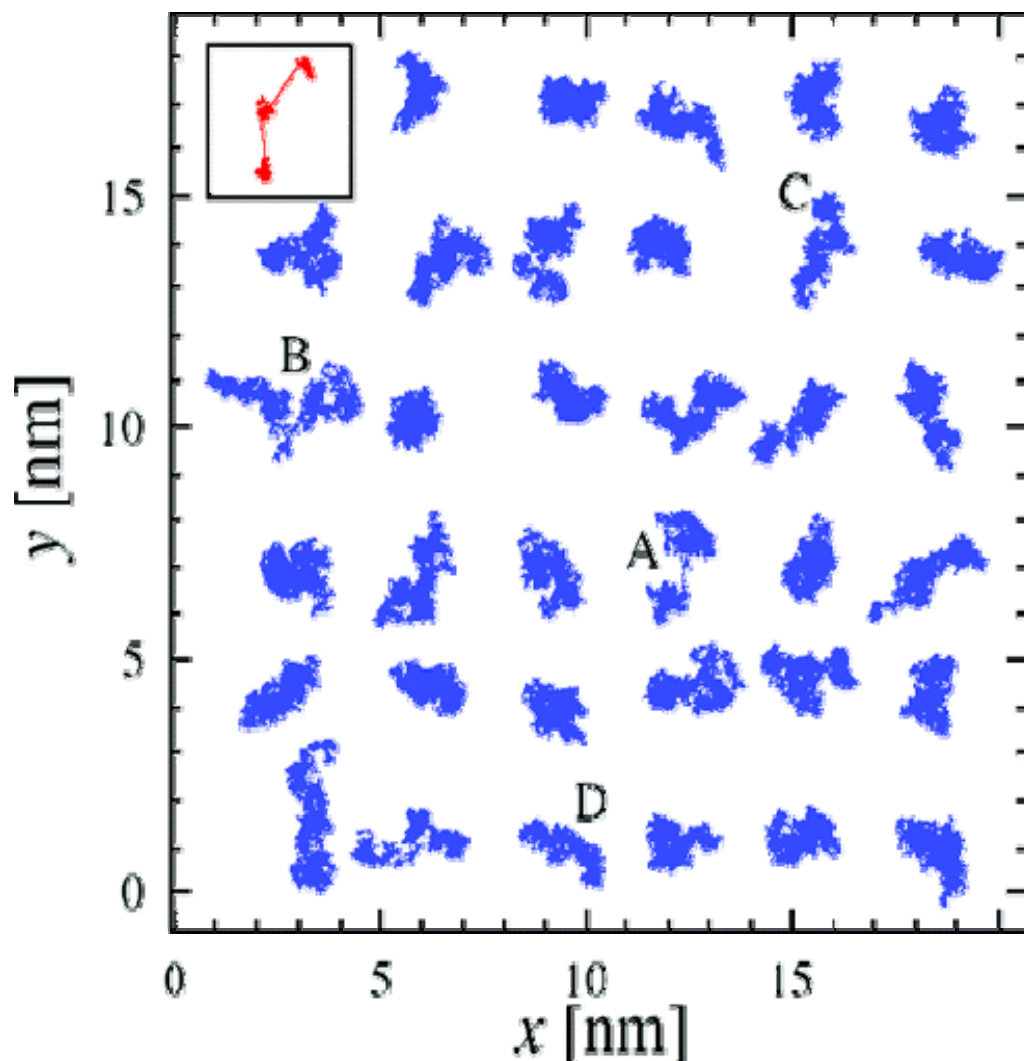
- 4 systems with number of lipids ranging between 128 - 4096
- Time scale 10 - 100 ns

Less than 10 events observed where a lipid moves ~ 0.7 nm in a short period of ~ 100 ps.

That is, the simulations indicate that there are no single-particle jumps

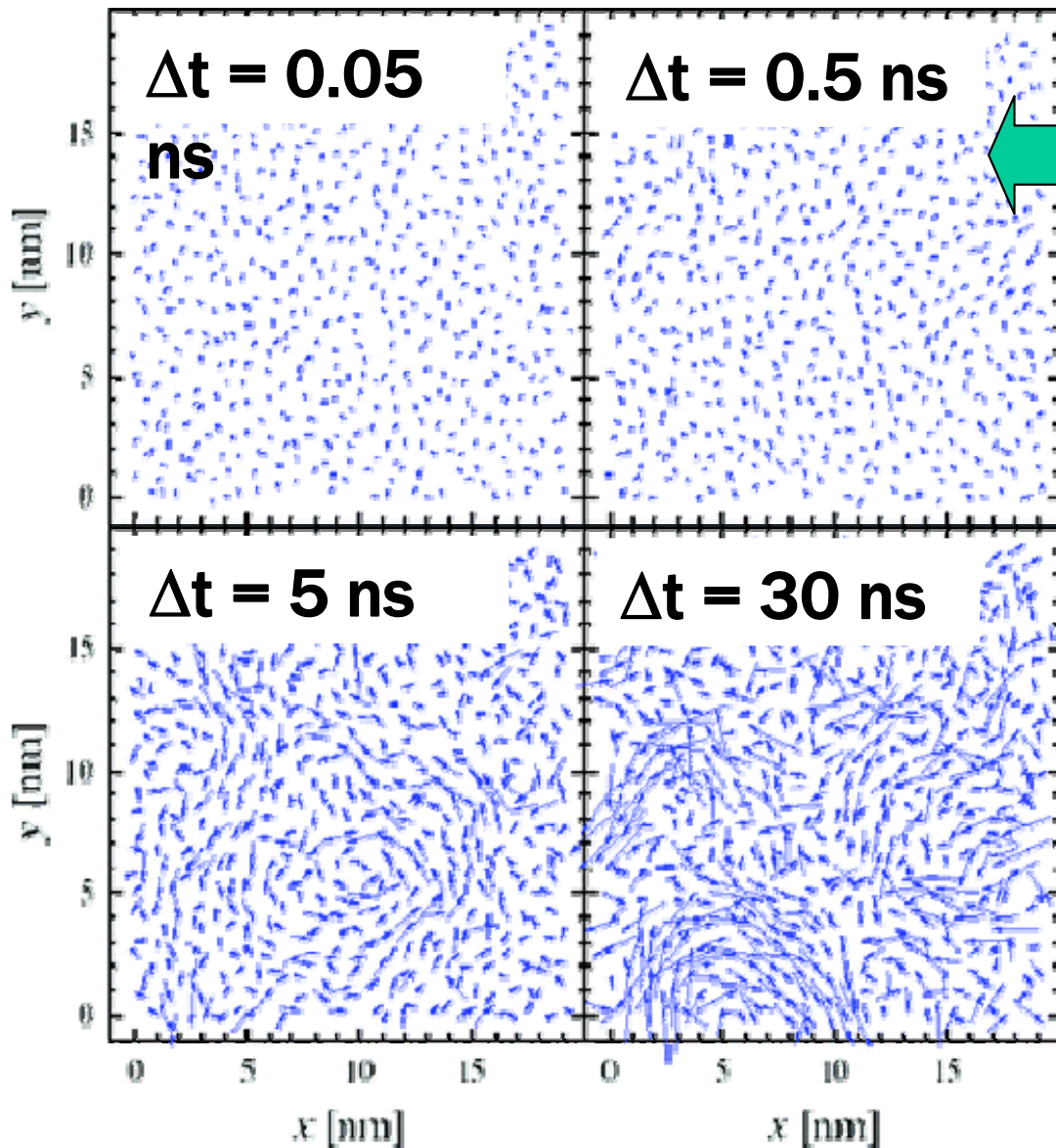
Lateral Lipid Diffusion Mechanism

Lateral lipid displacements over $\Delta t = 1$ ns



A more detailed consideration reveals that all diffusive motions are collective ones, as nearby lipids move in unison as loosely defined clusters.

Collective Diffusive Large-Scales Flows

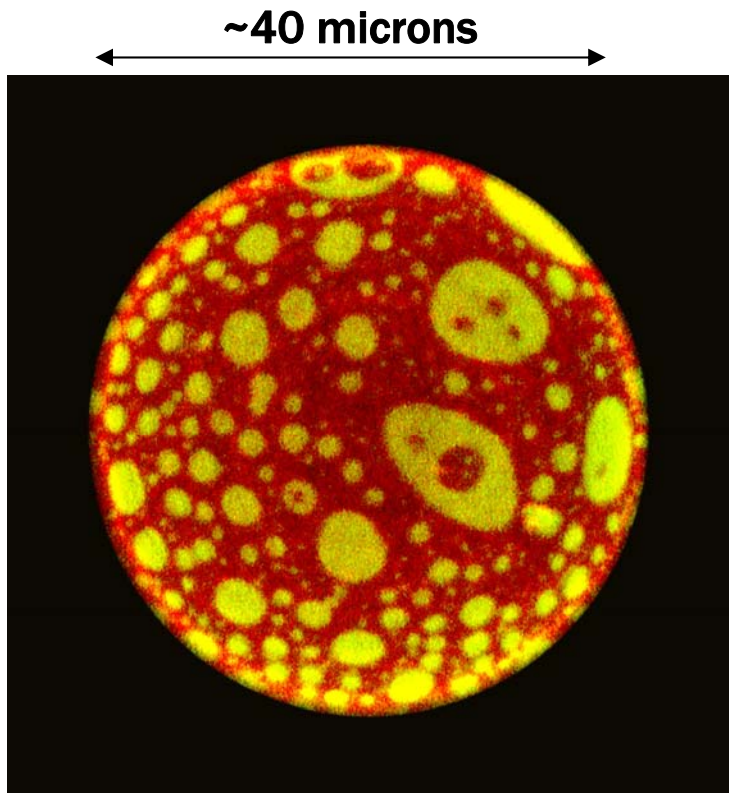


Lateral displacements of individual lipids during a period of Δt

On a molecular scale, lipids move in unison as loosely defined clusters.

On larger scales, the intimately correlated motions of neighboring lipids manifest themselves as **2D flow patterns**

Time Scales of Lateral Diffusion



www.memphys.sdu.dk

Time scale for diffusion over a domain whose radius is L

$$t = L^2 / 4D$$

In the fluid phase, $D \approx 1 \times 10^{-7} \text{ cm}^2/\text{s}$. Then the time scale t is at least

$$t = 2.5 \mu\text{s} \quad \text{for } L = 10 \text{ nm (nanorafts)}$$
$$25 \text{ ms} \quad \text{for } L = 1 \mu\text{m (large domains)}$$

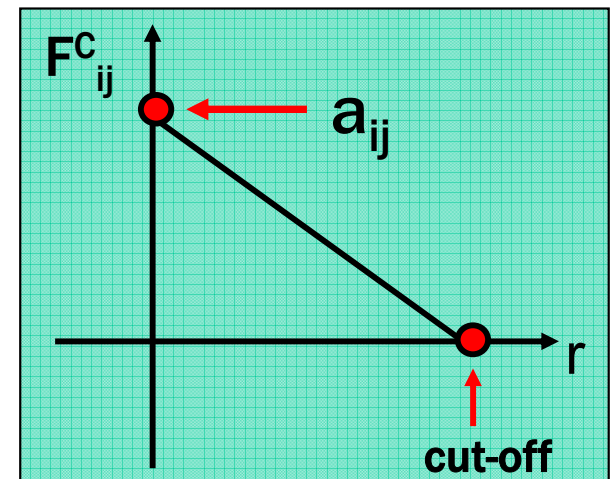
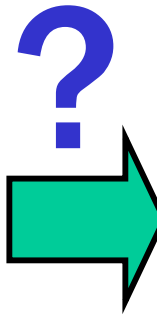
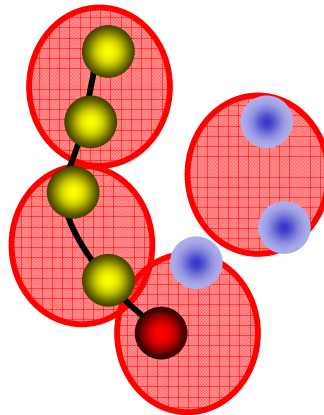
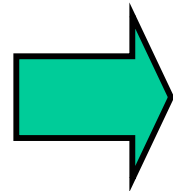
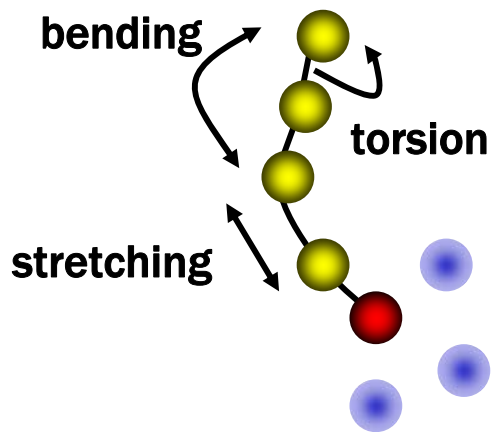
State-of-the-art atomistic simulations are limited to $\sim 0.1 \mu\text{s}$ and 10 nm.

Long time scales & the large system sizes call for coarse-grained models.

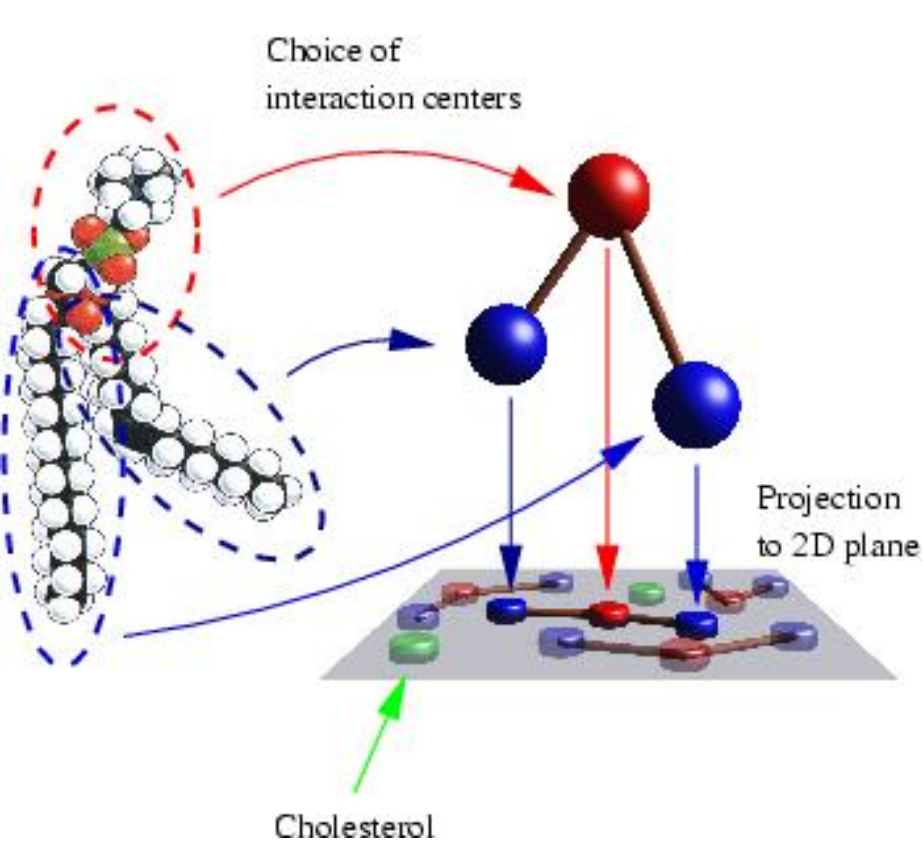
Effective Interactions?

How to find effective interactions for the CG model?

Systematic coarse graining through
Inverse Monte Carlo (IMC)



Coarse Grained Model: DPPC/Chol



Coarse-grained model system:

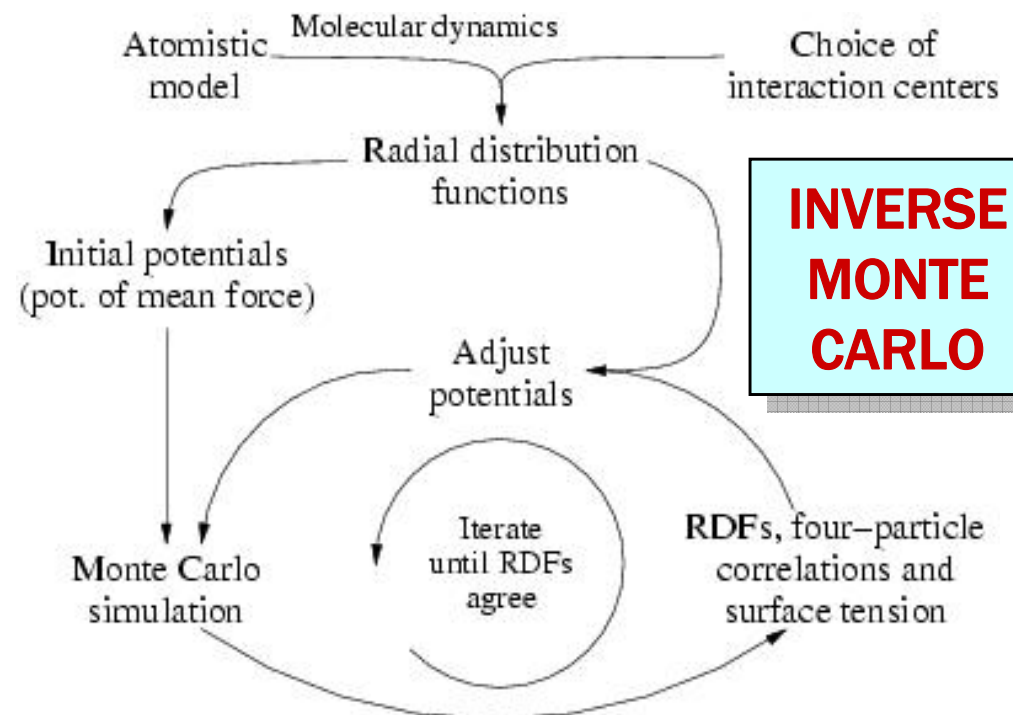
DPPC + Chol

No explicit water

Time: ~ms

$x_{\text{chol}} = 0 - 50 \text{ mol\%}$

Speed-up: $\sim 10^8$



For *Inverse Monte Carlo* (IMC), see Lyubartsev and Laaksonen, PRE 52, 3730-3737 (1995).

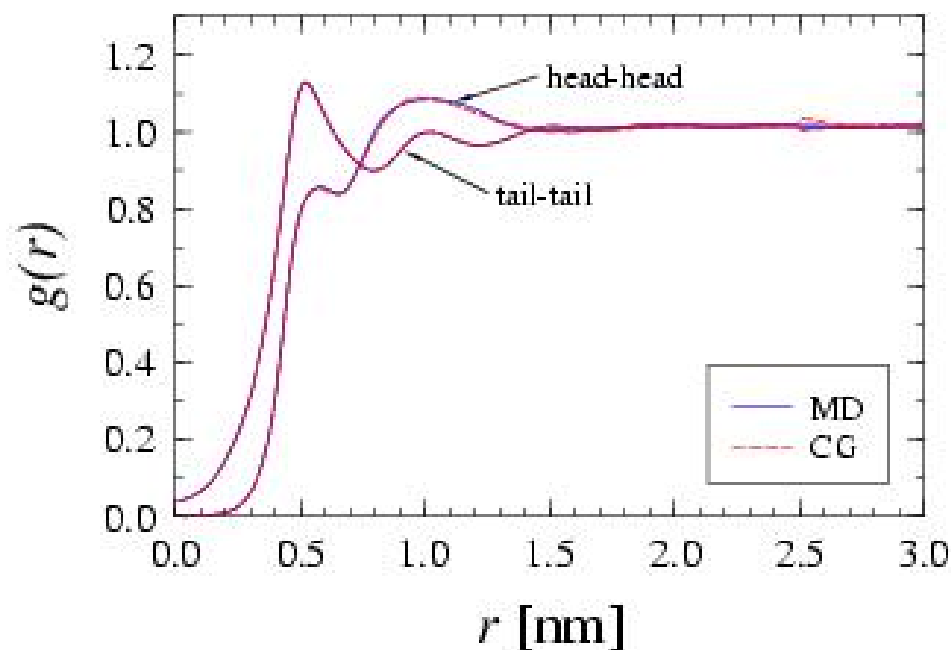
Main features:

1. 3-particle CG representation for DPPC
2. 1-particle CG representation for Chol
3. **Surface tension included** via Lagrange multipliers to match the area compressibility to the experimental value

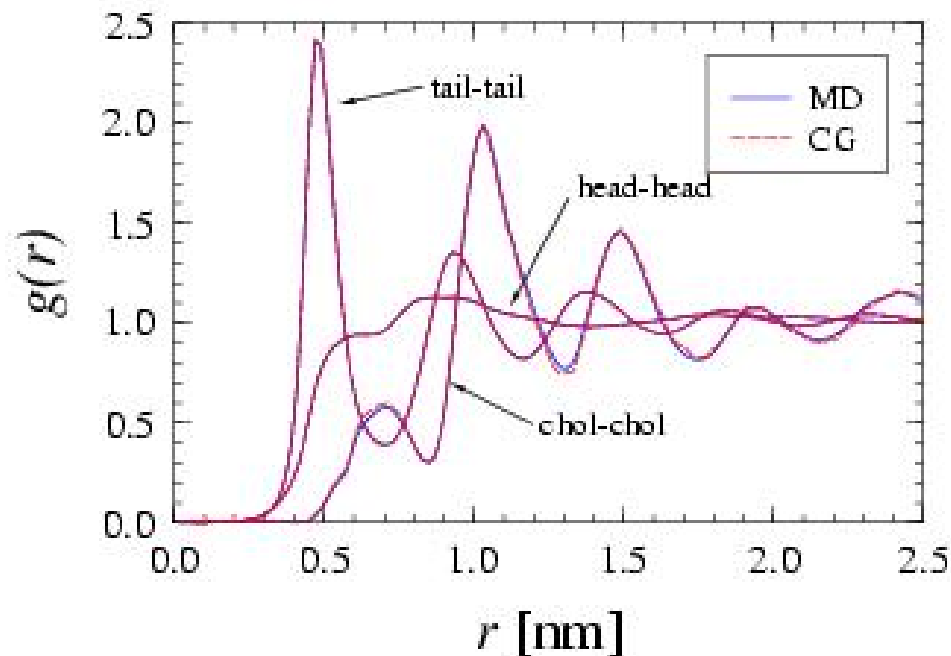
T. Murtola et al., J Chem Phys 126, 075101 (2007)

$g(r)$ from MD \rightarrow Effective potentials

Chol concentration 0%



Chol concentration 30%



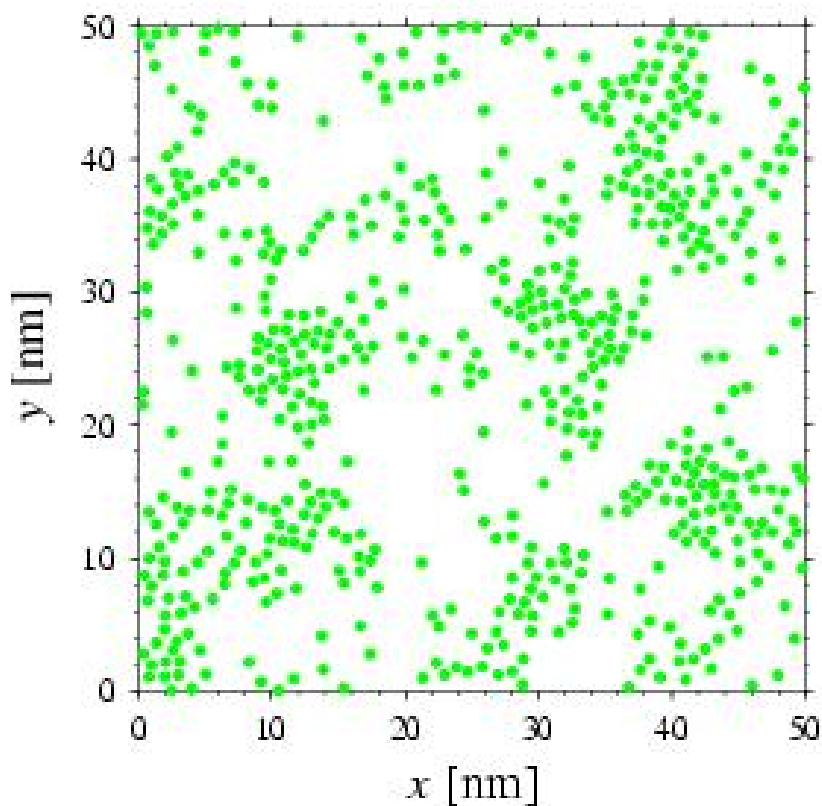
Radial distribution functions of the atom-scale and CG model match, as expected

Large-Scale Structures by CG Model

Snapshots from above: only positions of cholesterol molecules are shown here by green

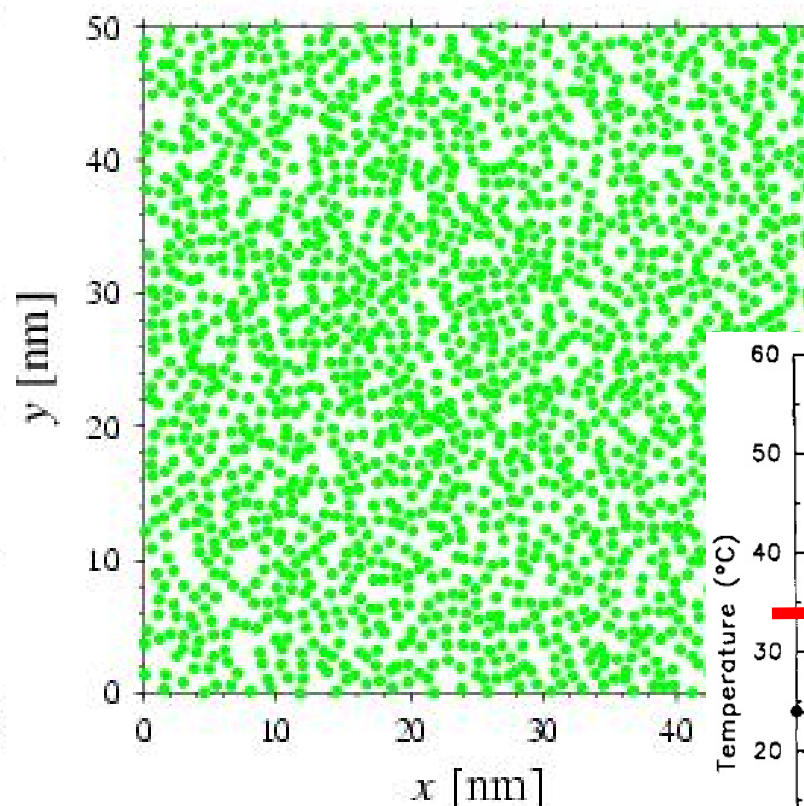
Experiments predict coexistence
of chol-rich and chol-poor domains

Chol concentration 13%

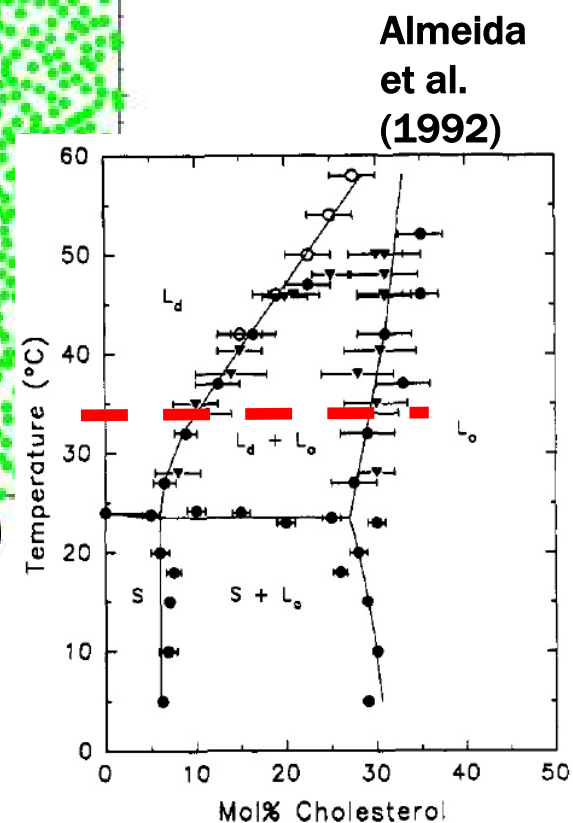


Experiments predict homogeneous
distribution of cholesterol

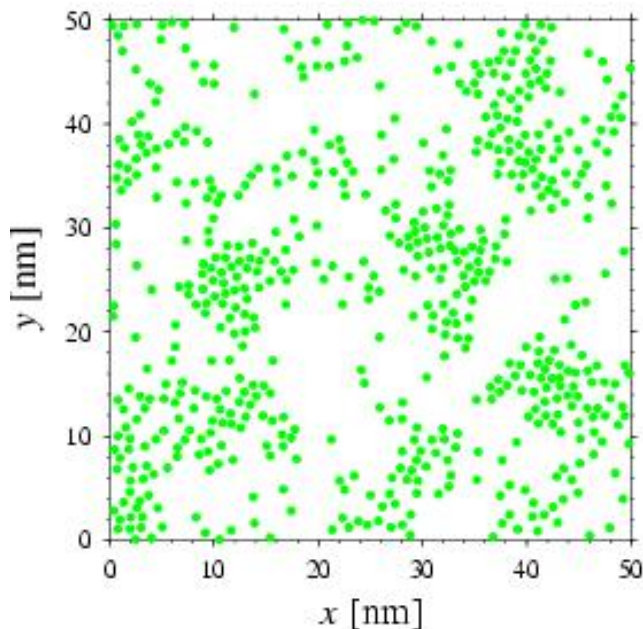
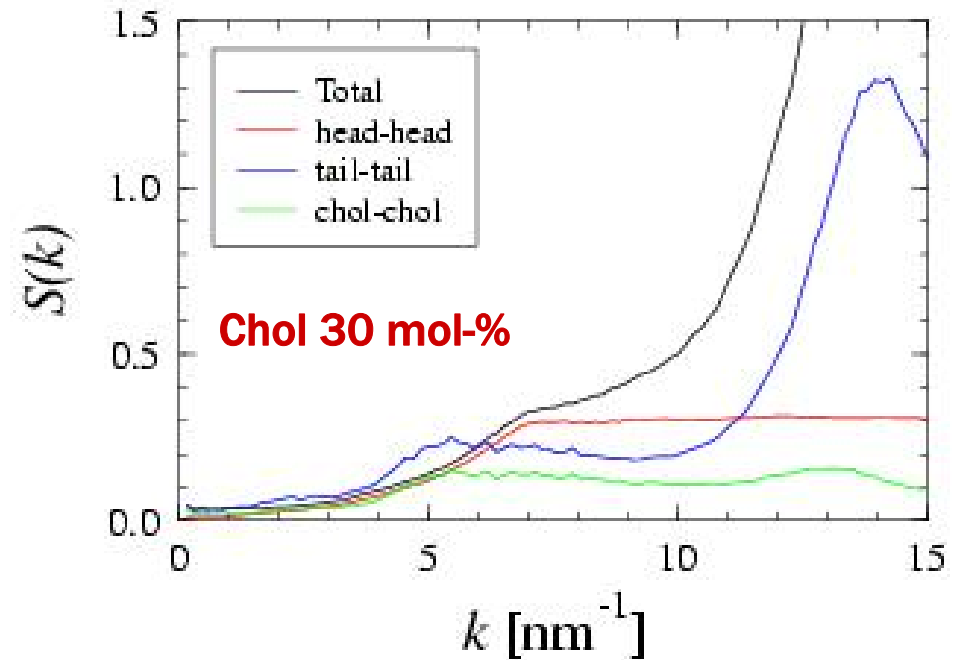
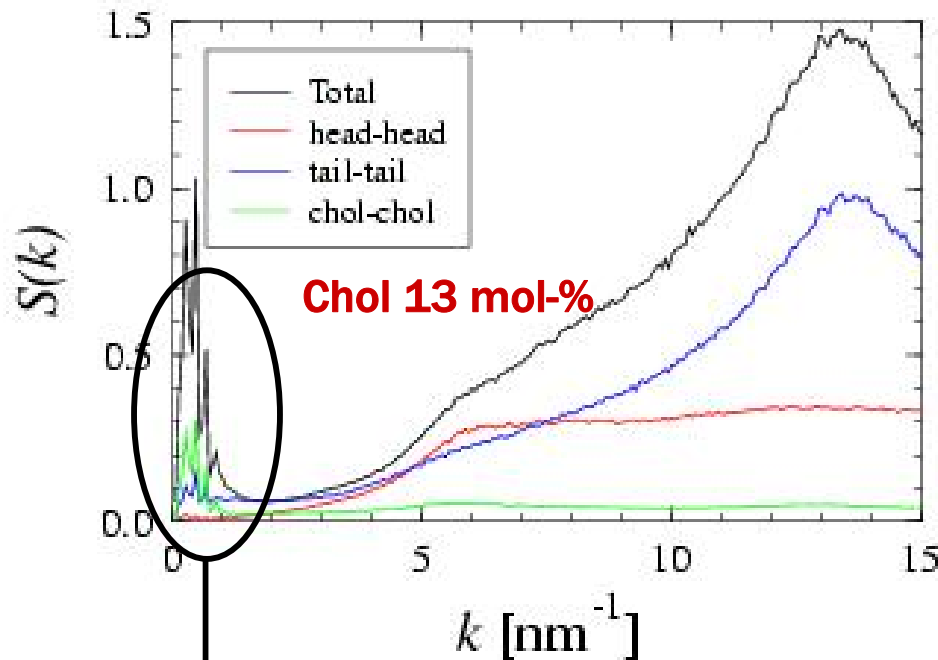
Chol concentration 30%



T. Murtola et al., *J Chem Phys* 126, 075101 (2007)



Static Structure Factors $S(k)$

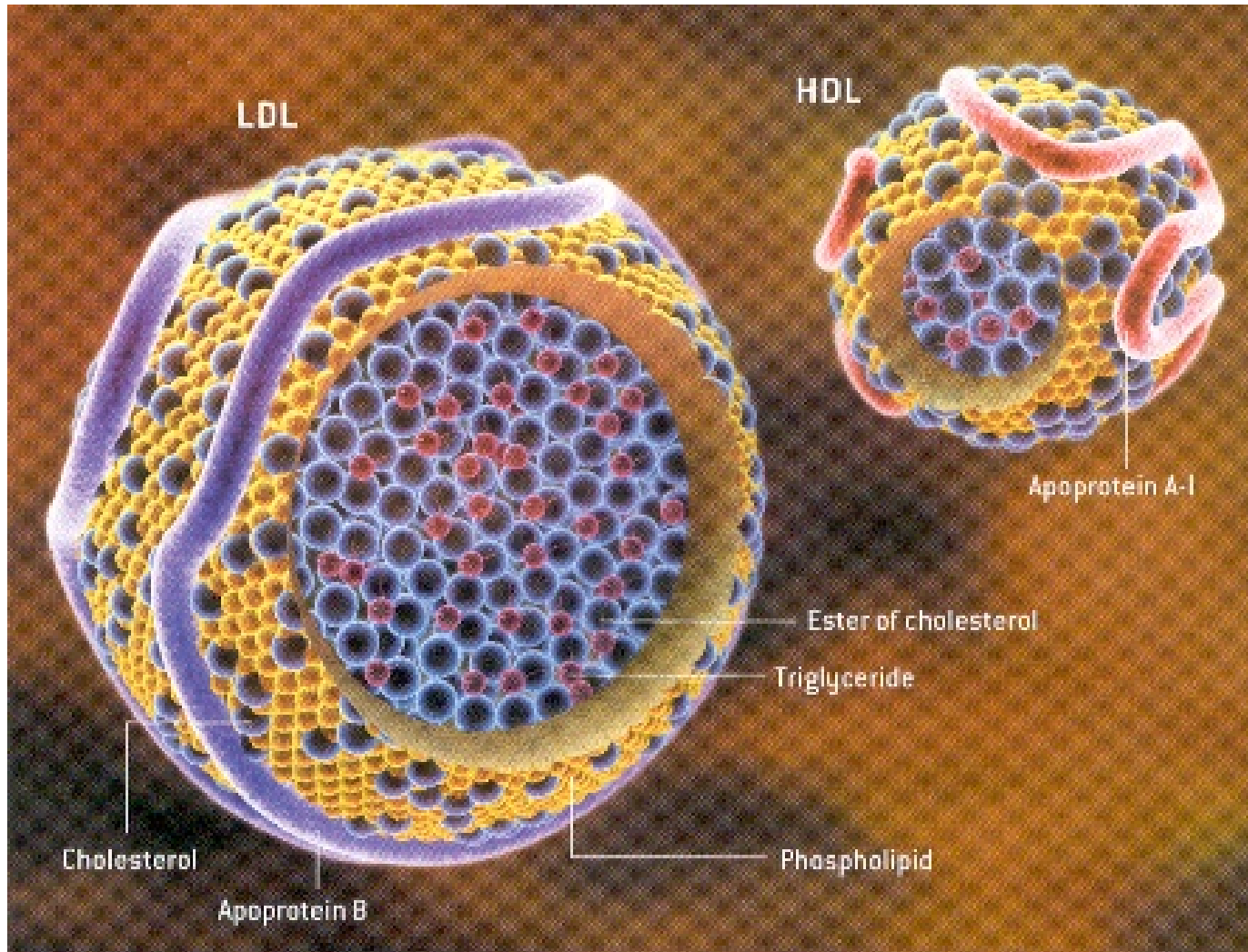
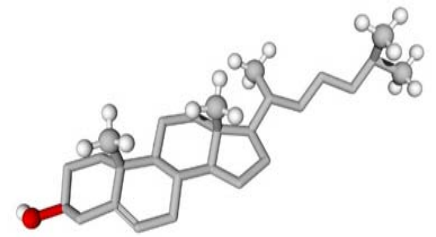


Main advantage of the CG model:

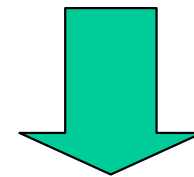
Elastic behavior in terms of area compressibility can be incorporated properly.

Large-scale domain ordering can be predicted

Lipoproteins, carriers of Chol



Suggestive views
for the structure
have been
proposed, but the
bottom line is that
the structures of
lipoproteins are
not known



**Functions of
lipoproteins are
not understood
either**

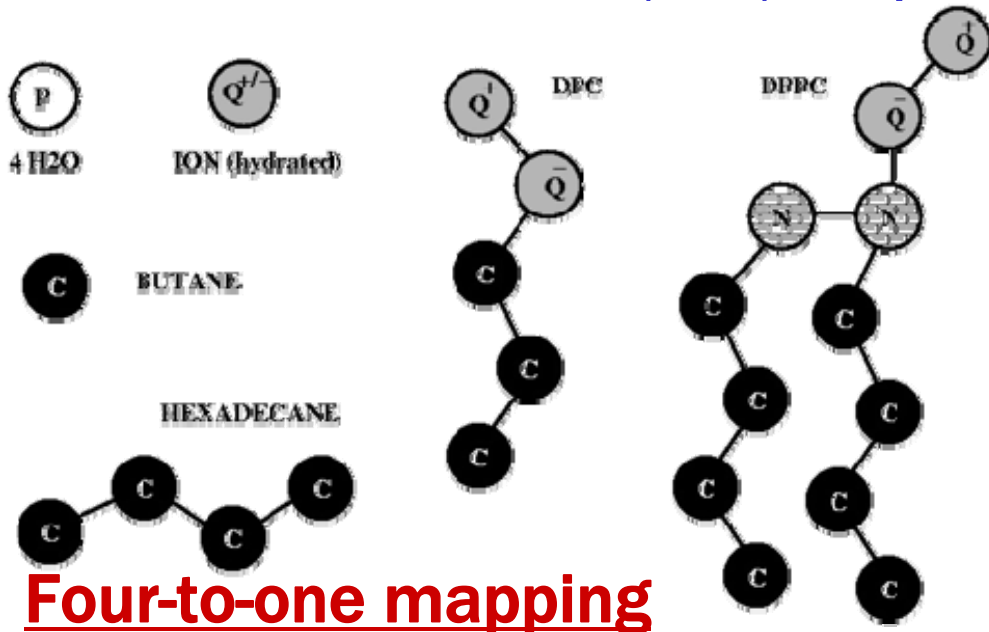
Scientific American (2004)

Coarse-Grained MD – MARTINI Model

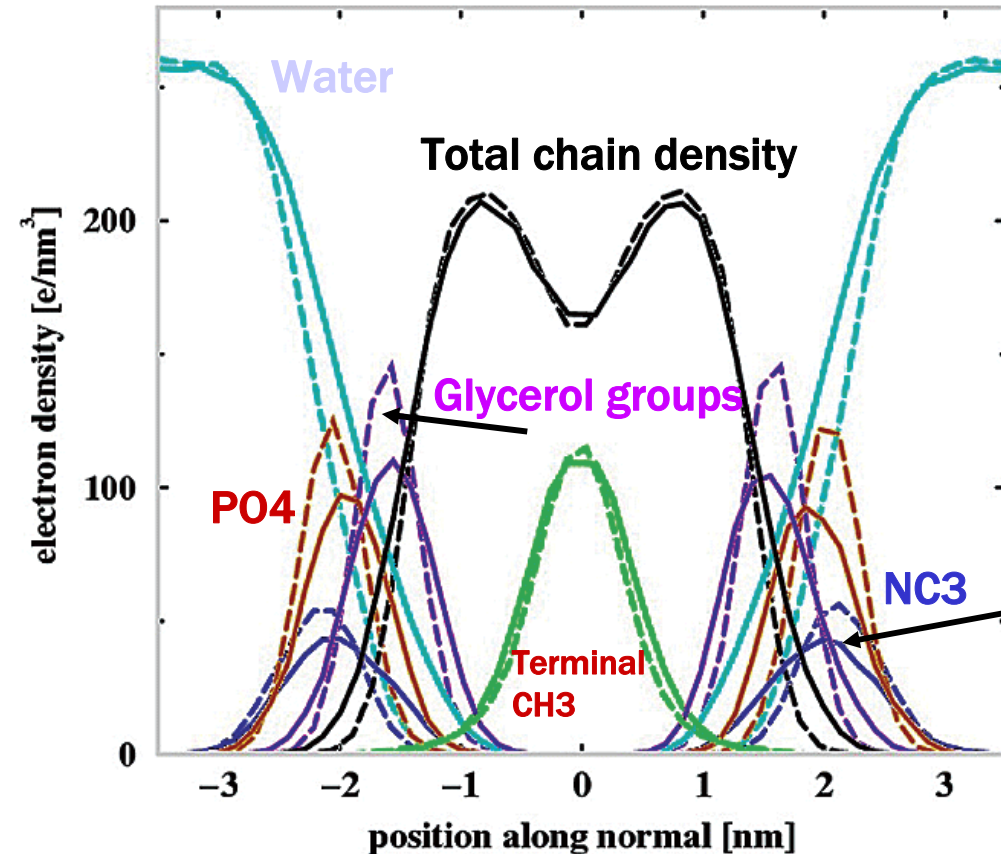
Classical Molecular Dynamics but now with coarse-grained beads and interactions instead of atomistic descriptions

Marrink et al., JPCB 108, 750 (2004)

Marrink et al., JPCB 111, 7812 (2007); & In press.

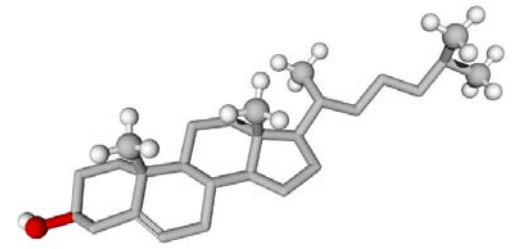


Interaction parameters are chosen such that oil-water partitioning free energies are described properly by the CG model with respect to experimental data.



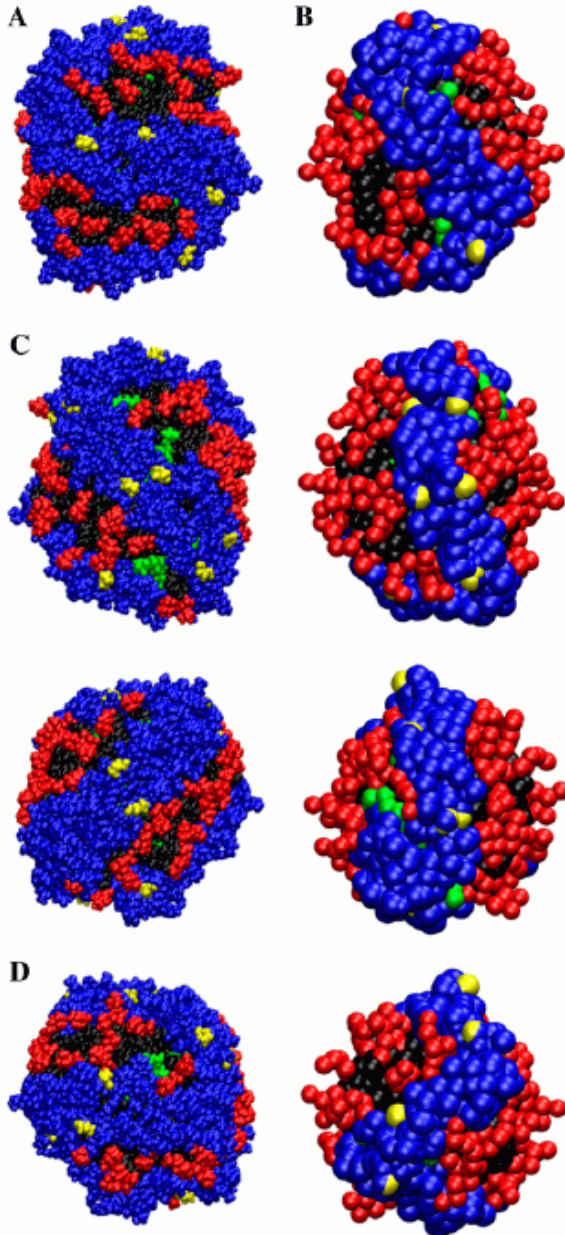
Density profiles of different components across the lipid membrane – comparison between atomistic and CG model results.

HDL – “Good” cholesterol



Atomistic

CG



Model:

2 ApoA-I –proteins

56 POPC

16 Cholesterol oleates

Atomistic simulations:

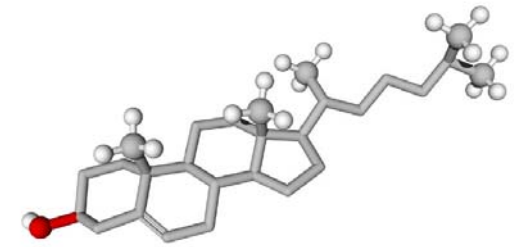
~10 ns, CHARMM force fields

CG simulations

~1 microsecond, MARTINI model by Siewert-Jan Marrink, Luca Monticelli et al.

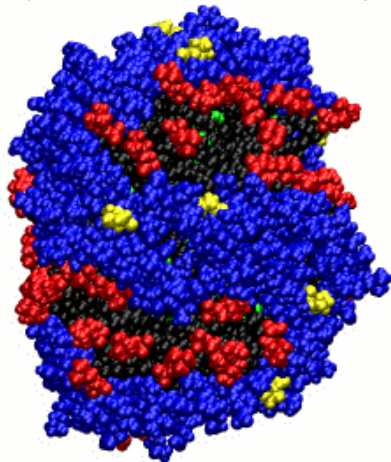
Structure of spheroidal HDL particles revealed by Combined Atomistic and Coarse Grained Simulations.
A. Catte et al., *Biophys. J.* 94, 2306 (2008).

HDL – "Good" cholesterol



AA

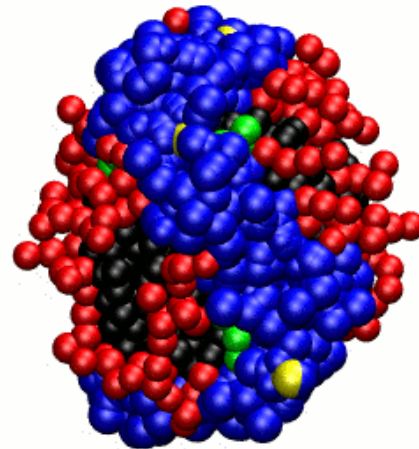
10 ns at 310K



Atomistic model for
High Density
Lipoprotein

CG

1 μs at 310K



Coarse Grained
model for High
Density Lipoprotein

TABLE 1 Components of the moments of inertia (I) and values of semiaxes (a – c) of ms-HDL particles from atomistic and CG MD simulations

I (kg/Å ² /10 ⁻³)* a , b , and c (Å)*	Particle	
	10 ns at 310 K (10 ns at 410 K)	1 μs at 310 K
I_{xx}	61.1 ± 0.6	23.3 ± 0.8 [†]
I_{yy}	55.6 ± 0.6	17.8 ± 0.4 [†]
I_{zz}	43.5 ± 0.5	14.2 ± 0.4 [†]
a	31.0 ± 0.3	26.4 ± 0.9
b	35.2 ± 0.3	39.8 ± 1.3
c	42.9 ± 0.4	46.5 ± 0.8

**Coarse Grained model describes HDL
shape and size very well**

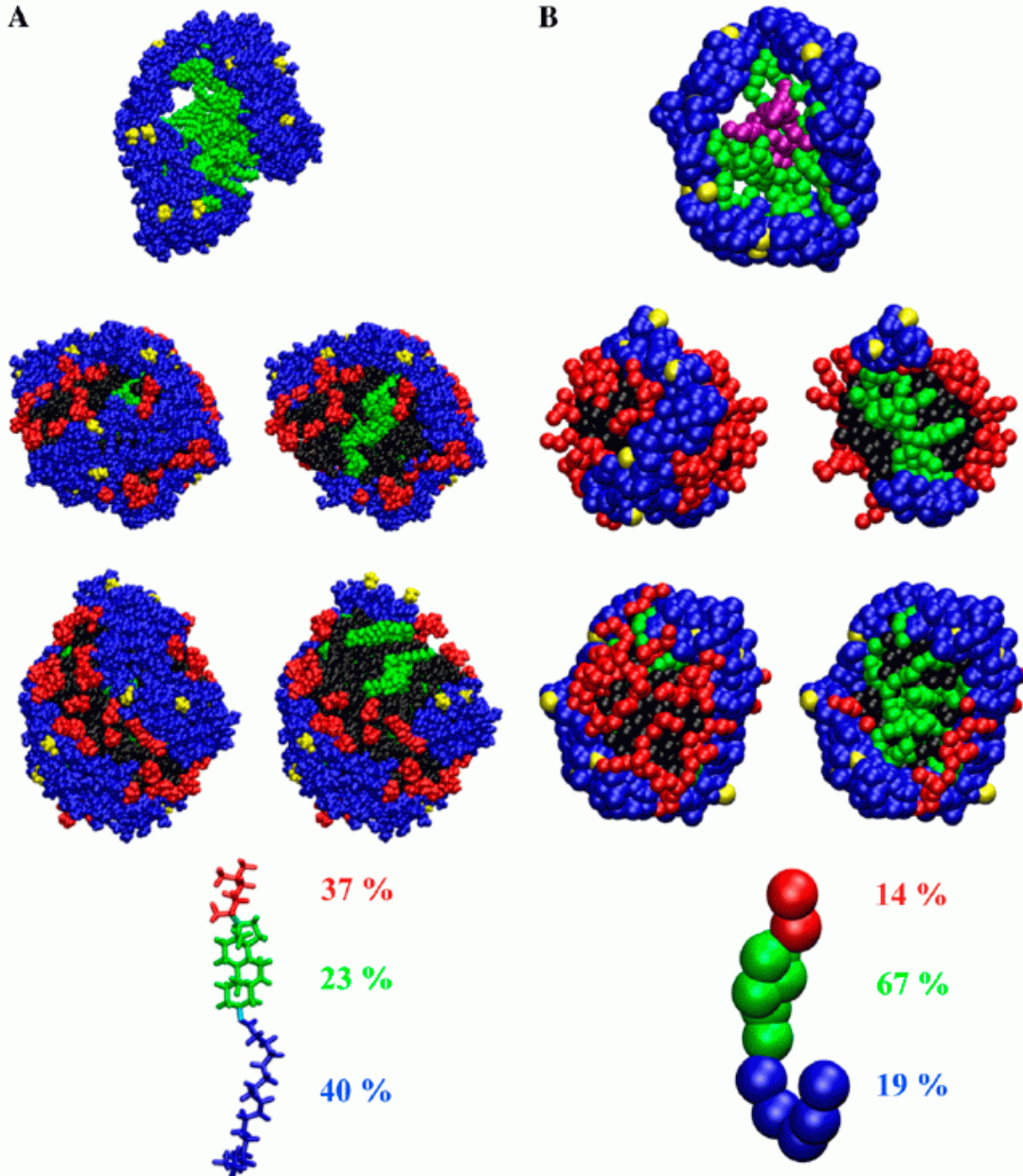
Structure of spheroidal HDL particles revealed by Combined Atomistic and Coarse Grained Simulations.

A. Catte et al., Biophys. J. 94, 2306 (2008).

Novel Changes in Discoidal High Density Lipoprotein Morphology: A Molecular Dynamics Study.

A. Catte et al., Biophys. J. 90, 4345 (2006).

HDL – "Good" cholesterol



Annular cholesterol esters
(green) in contact with apoA-I:
Almost 100%

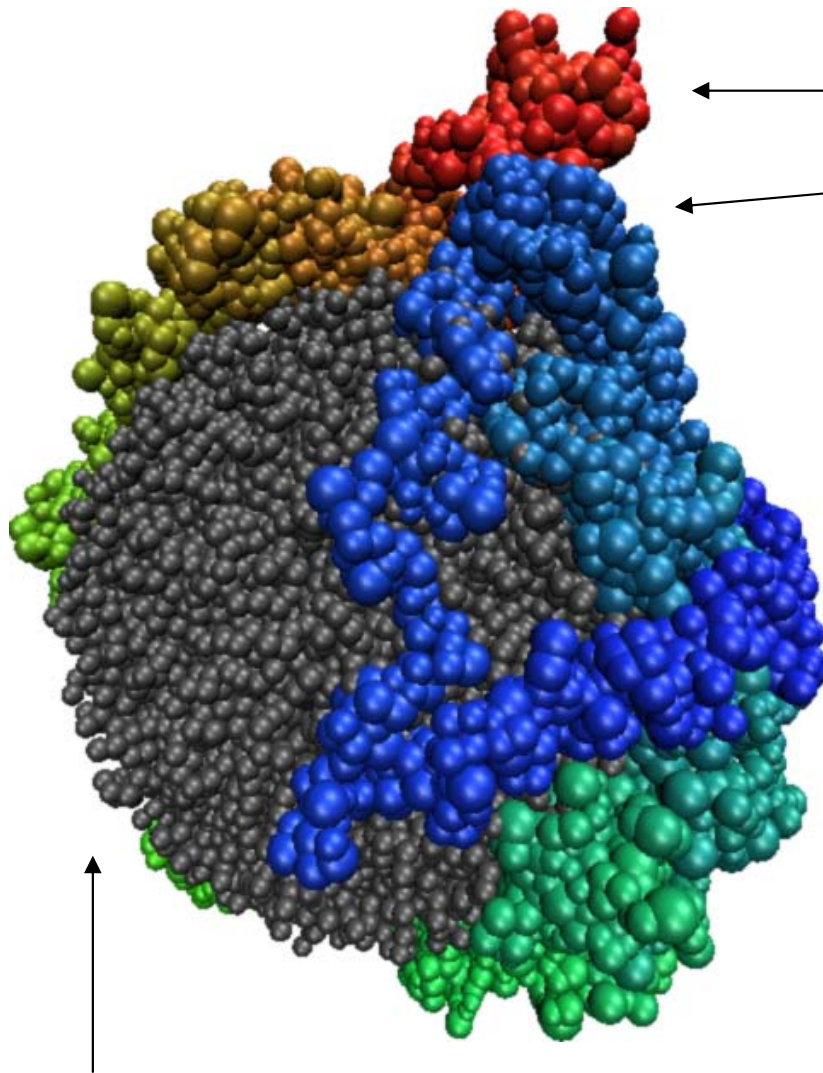
Packing of cholesterol esters
(green) within POPCs

Chol esters stabilizing
apoA-I and thus HDL

Almost 100% of chol esters are
annular.

Atomistic and CG models
roughly consistent regarding
contacts, the differences due
to the CG nature of beads

LDL – “Bad” Cholesterol



Complex lipid
droplet (gray)

← N-terminal of apoB-100

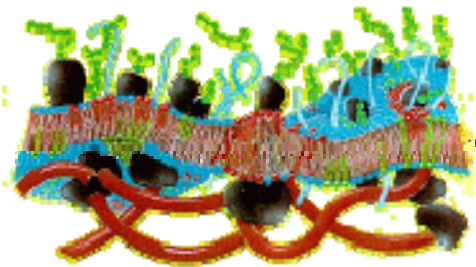
← C-terminal

Coarse-grained modeling of LDL-sized lipid droplets with molecular composition consistent with experimental data – model designed bottom-up using extensive atomistic simulation data of our own.

T. Murtola, T. Vuorela et al.,
work in progress (2007-2008).

Why coarse-grained simulations?

- Atomistic simulations for LDL over 1 μ s would take ~100 CPU-years
- We need time scales > 10 μ s...



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