



Mixed mode in CASINO

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Experts in numerical algorithms
and HPC services

Outline

- Introduction
- OpenMP sectors
 - One particle orbitals
 - Jastrow
 - Ewald
 - Update \bar{D}
 - e-e relative distances
- Performance results and discussion

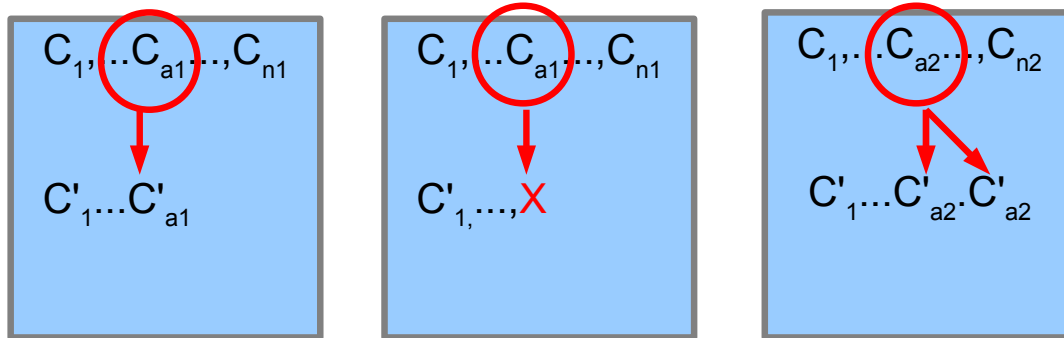
Introduction I

- CASINO is Quantum Monte Carlo code used to compute electronic structure properties of large molecules or solids.
- It scales up to 40,000 cores.
- For models with large number of electrons one configuration computation needs to be accelerated (N^2 scaling).

CASINO is developed by TCM group, Cambridge University.

<http://www.tcm.phy.cam.ac.uk/~mdt26/casino2.htm>

Introduction II



$$t = N_{step} \times \frac{N_{pop}}{P} \times \frac{t_{config}}{N_{thread}} \quad t_{config} \sim N_e^2$$

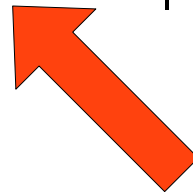
Numerical kernels: OPO

$$i\hbar \frac{\partial \Psi(R, t)}{\partial t} = -\frac{\hbar^2}{2m} \sum_{i=1}^{N_e} \nabla_i^2 \Psi(R, t) + V(R, R_I) \Psi(R, t)$$

$$D_{\uparrow} = \begin{vmatrix} \phi_1(r_1) & \phi_1(r_2) & \cdots & \phi_1(r_{N_{\uparrow}}) \\ \vdots & \cdots & \cdots & \vdots \\ \phi_{N_{\uparrow}}(r_1) & \phi_{N_{\uparrow}}(r_2) & \cdots & \phi_{N_{\uparrow}}(r_{N_{\uparrow}}) \end{vmatrix}$$

$$\Psi = e^{J(\alpha, R, R_I)} D_{\uparrow} D_{\downarrow}$$

$$J(R) = \sum_{\substack{i < j, \\ \sigma_i, \sigma_j}} u_{\sigma_i, \sigma_j}(\alpha, |r_i - r_j|)$$



One particle orbital (OPO)

Numerical kernels: JASTROW

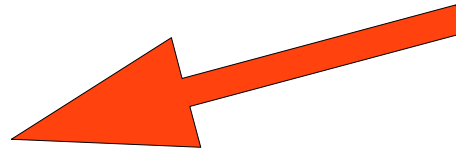
$$i\hbar \frac{\partial \Psi(R, t)}{\partial t} = -\frac{\hbar^2}{2m} \sum_{i=1}^{N_e} \nabla_i^2 \Psi(R, t) + V(R, R_I) \Psi(R, t)$$

$$D_{\uparrow} = \begin{vmatrix} \phi_1(r_1) & \phi_1(r_2) & \cdots & \phi_1(r_{N_{\uparrow}}) \\ \vdots & \cdots & \cdots & \vdots \\ \phi_{N_{\uparrow}}(r_1) & \phi_{N_{\uparrow}}(r_2) & \cdots & \phi_{N_{\uparrow}}(r_{N_{\uparrow}}) \end{vmatrix}$$

Jastrow (JAS)

$$\Psi = e^{J(\alpha, R, R_I)} D_{\uparrow} D_{\downarrow}$$

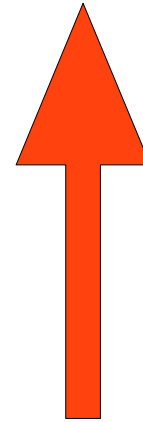
$$J(R) = \sum_{\substack{i < j, \\ \sigma_i, \sigma_j}} u_{\sigma_i, \sigma_j}(\alpha, |r_i - r_j|)$$



Numerical kernels: Ewald summation

$$i\hbar \frac{\partial \Psi(R, t)}{\partial t} = -\frac{\hbar^2}{2m} \sum_{i=1}^{N_e} \nabla_i^2 \Psi(R, t) + V(R, R_I) \Psi(R, t)$$

$$D_{\uparrow} = \begin{vmatrix} \phi_1(r_1) & \phi_1(r_2) & \cdots & \phi_1(r_{N_{\uparrow}}) \\ \vdots & \cdots & \cdots & \vdots \\ \phi_{N_{\uparrow}}(r_1) & \phi_{N_{\uparrow}}(r_2) & \cdots & \phi_{N_{\uparrow}}(r_{N_{\uparrow}}) \end{vmatrix}$$



Ewald Summation (EWA)

$$\Psi = e^{J(\alpha, R, R_I)} D_{\uparrow} D_{\downarrow}$$

$$J(R) = \sum_{\substack{i < j, \\ \sigma_i, \sigma_j}} u_{\sigma_i, \sigma_j}(\alpha, |r_i - r_j|)$$

Numerical kernels: Update D

$$i \hbar \frac{\partial \Psi(R, t)}{\partial t} = -\frac{\hbar^2}{2m} \sum_{i=1}^{N_e} \nabla_i^2 \Psi(R, t) + V(R, R_I) \Psi(R, t)$$

$$D_{\uparrow} = \begin{vmatrix} \phi_1(r_1) & \phi_1(r_2) & \cdots & \phi_1(r_{N_{\uparrow}}) \\ \vdots & \cdots & \cdots & \vdots \\ \phi_{N_{\uparrow}}(r_1) & \phi_{N_{\uparrow}}(r_2) & \cdots & \phi_{N_{\uparrow}}(r_{N_{\uparrow}}) \end{vmatrix}$$

$$\Psi = e^{J(\alpha, R, R_I)} D_{\uparrow} D_{\downarrow} \quad \leftarrow \text{Update } \bar{D} \text{ (} \bar{D} \text{)}$$

$$J(R) = \sum_{\substack{i < j, \\ \sigma_i, \sigma_j}} u_{\sigma_i, \sigma_j}(\alpha, |r_i - r_j|)$$

Numerical kernels: R_{ee}

$$i\hbar \frac{\partial \Psi(R, t)}{\partial t} = -\frac{\hbar^2}{2m} \sum_{i=1}^{N_e} \nabla_i^2 \Psi(R, t) + V(R, R_I) \Psi(R, t)$$

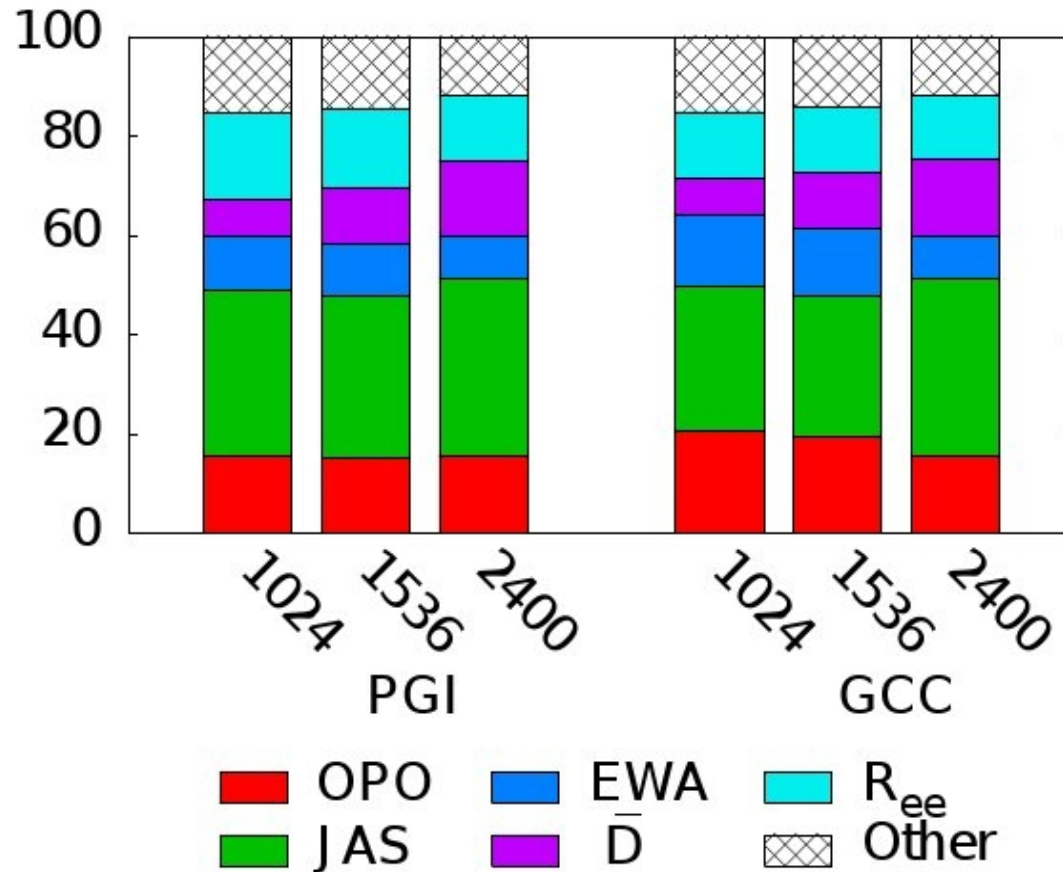
$$D_{\uparrow} = \begin{vmatrix} \phi_1(r_1) & \phi_1(r_2) & \cdots & \phi_1(r_{N_{\uparrow}}) \\ \vdots & \cdots & \cdots & \vdots \\ \phi_{N_{\uparrow}}(r_1) & \phi_{N_{\uparrow}}(r_2) & \cdots & \phi_{N_{\uparrow}}(r_{N_{\uparrow}}) \end{vmatrix}$$

$$\Psi = e^{J(\alpha, R, R_I)} D_{\uparrow} D_{\downarrow}$$

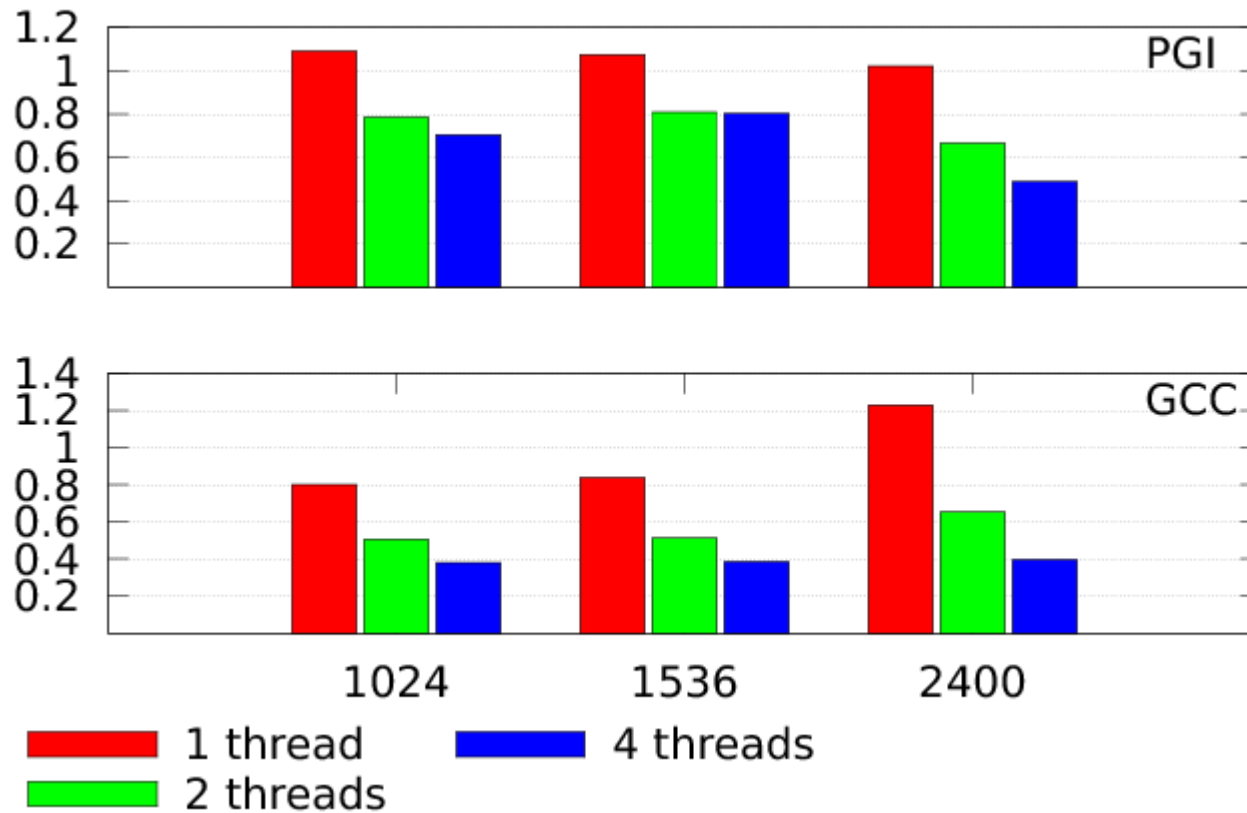
$$J(R) = \sum_{\substack{i < j, \\ \sigma_i, \sigma_j}} u_{\sigma_i, \sigma_j}(\alpha, |r_i - r_j|)$$

e-e distances (R_{ee})

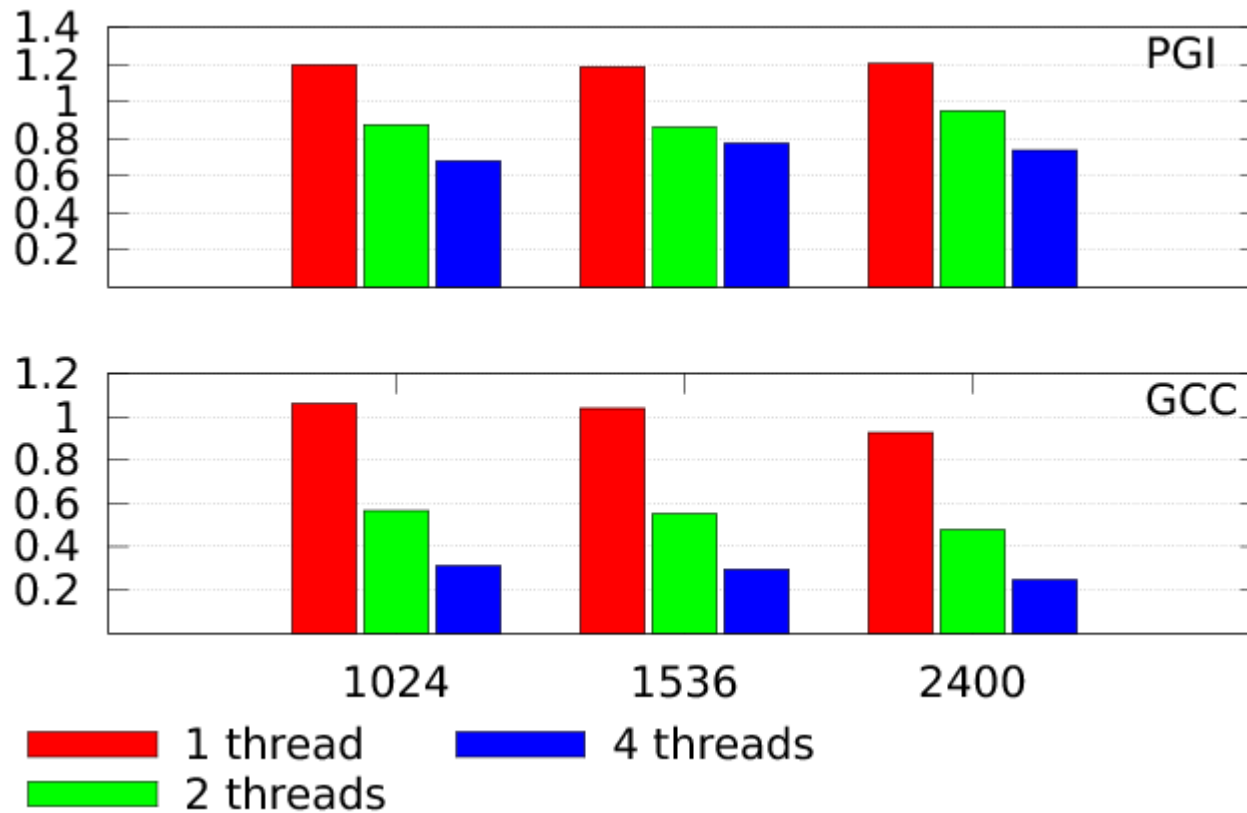
Time consumed by numerical kernels



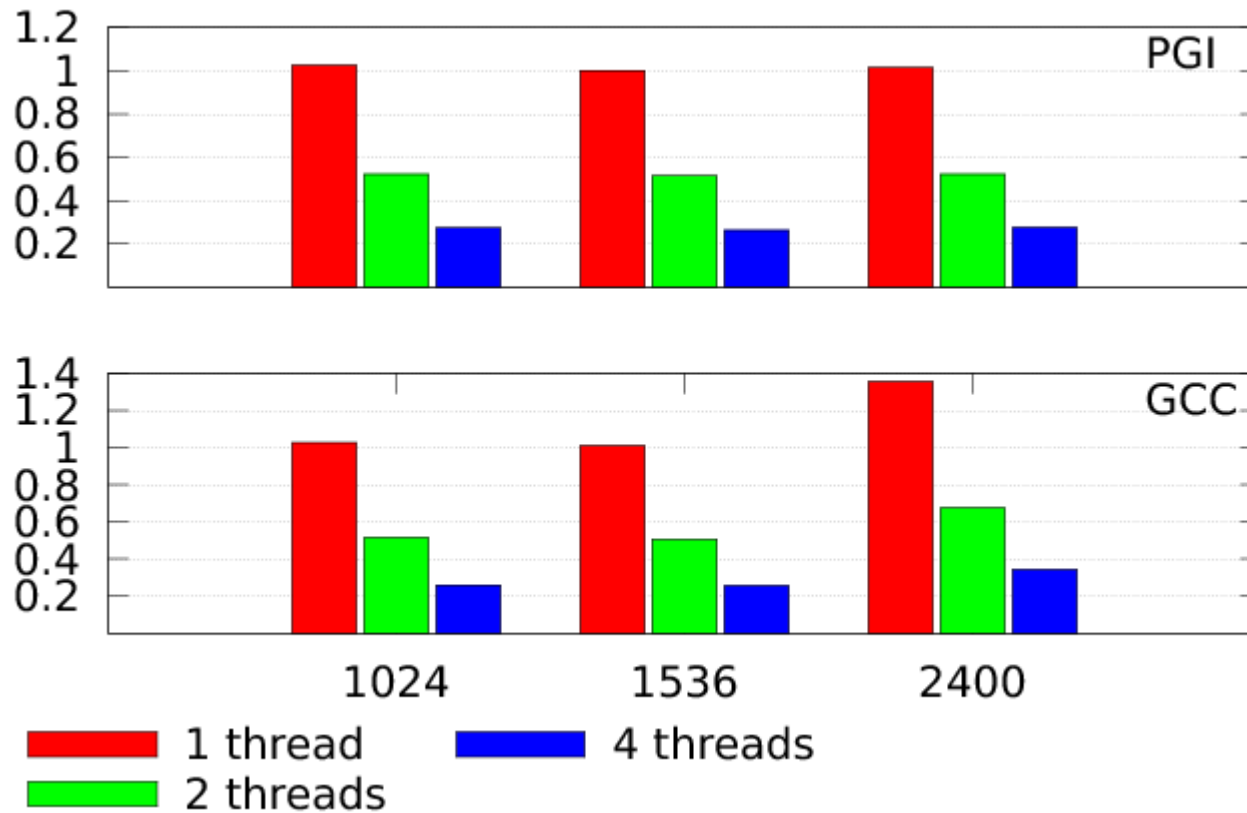
OPO



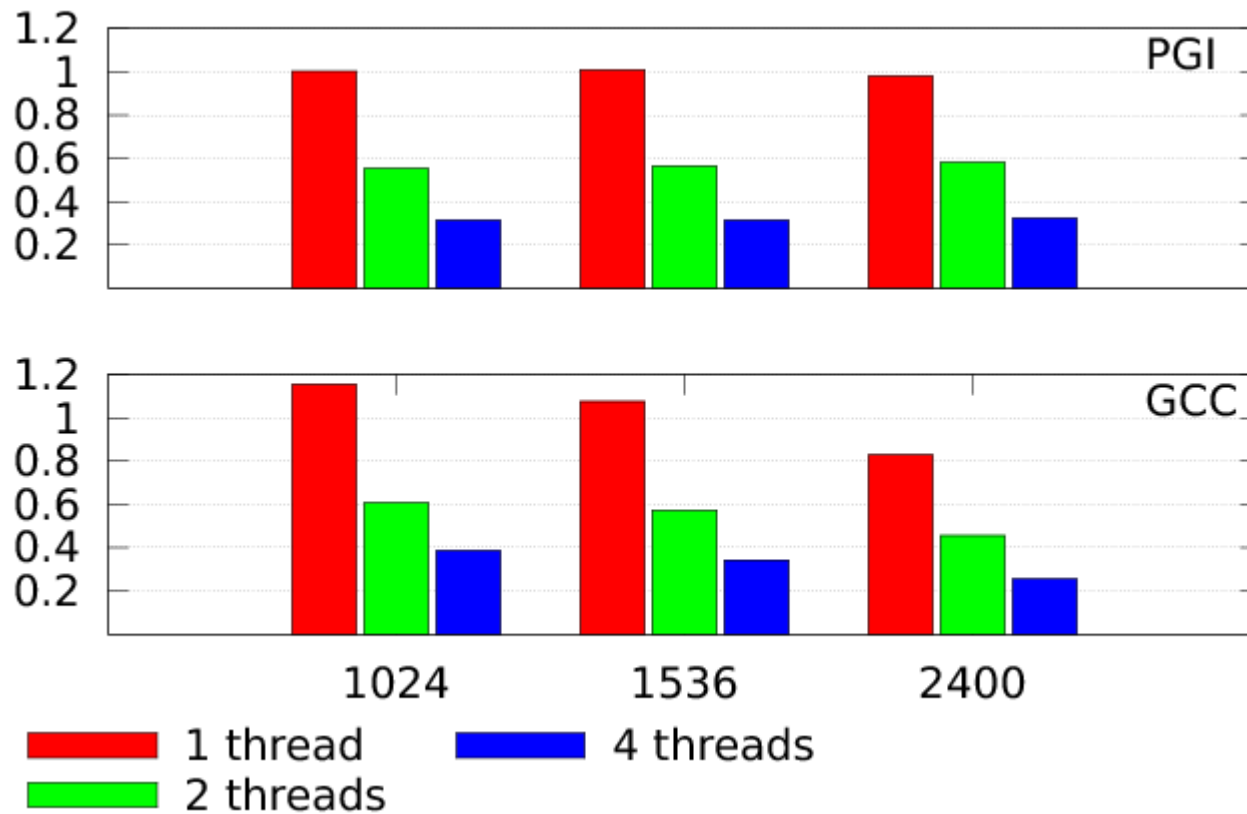
Jastrow



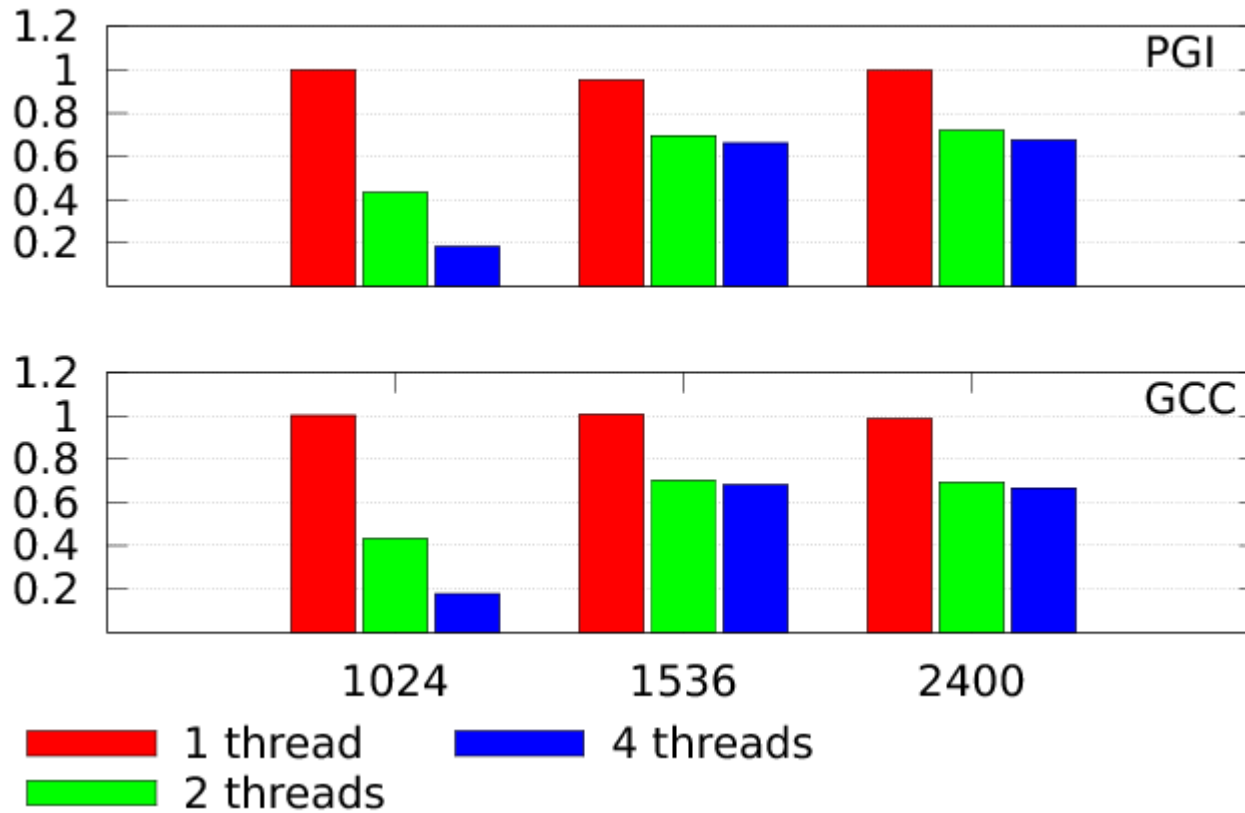
Ewald



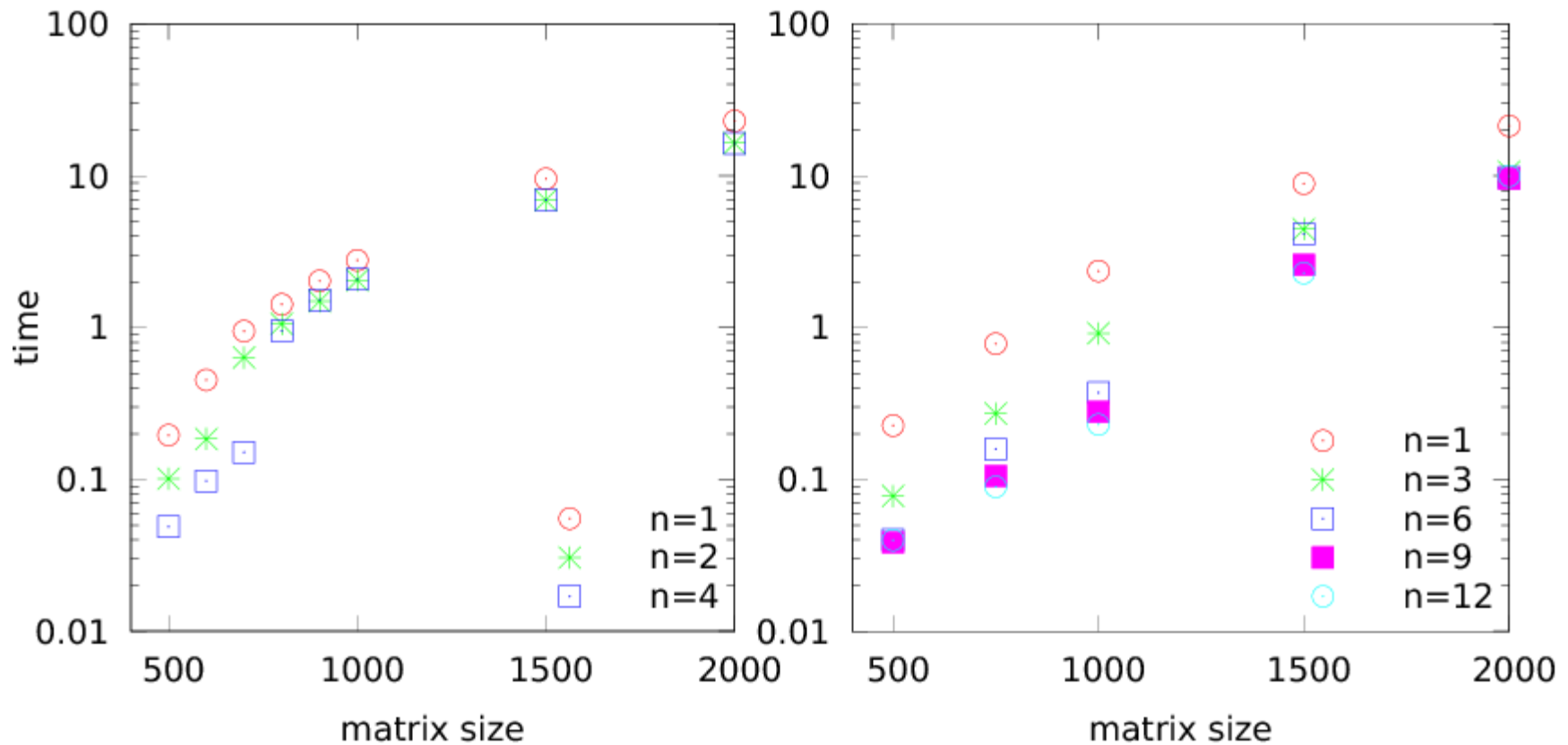
R_{ee}



\bar{D} matrix



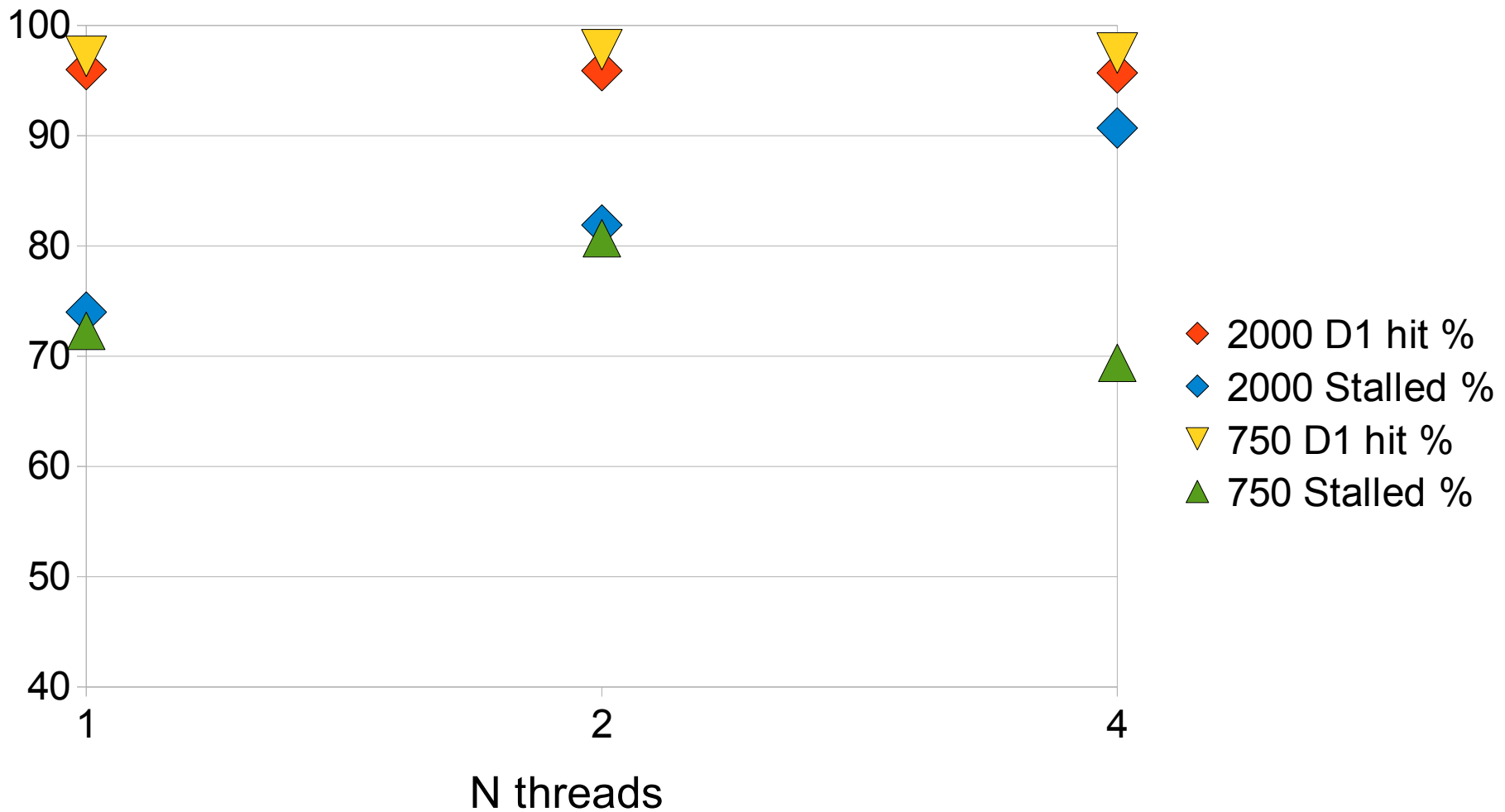
Scaling loss in matrix \bar{D} computation



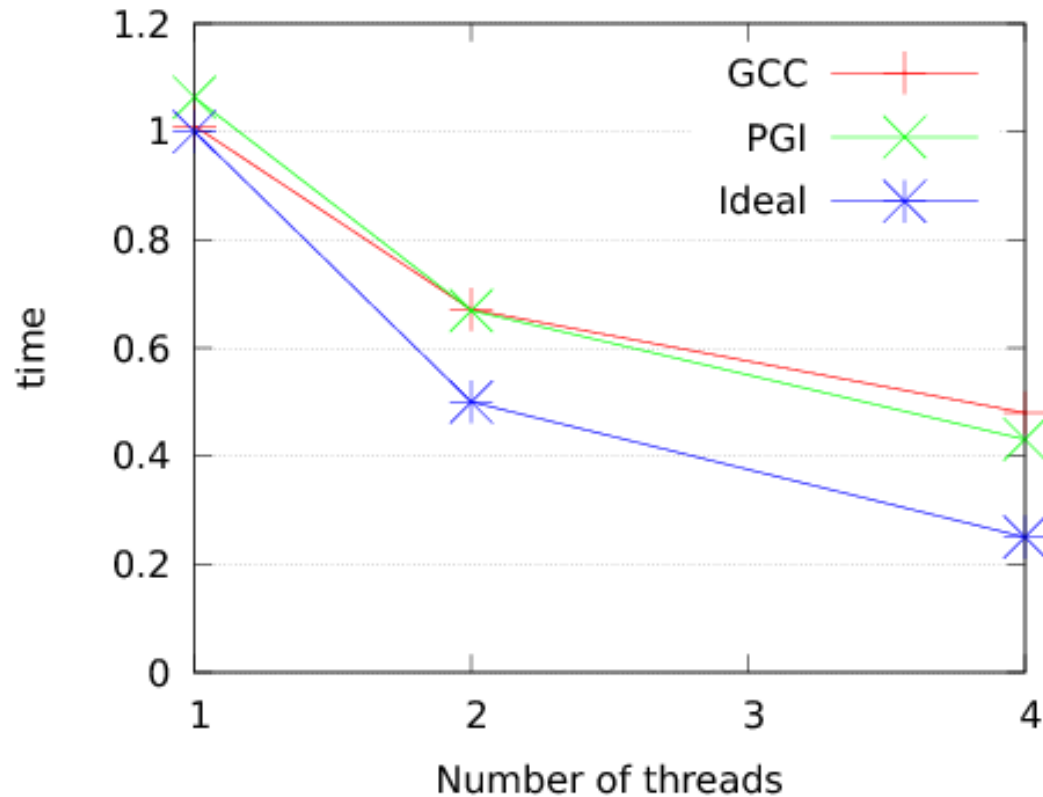
$$\sqrt{(4L_2 + L_3)/8} \approx 724$$

$$\sqrt{(6L_2 + L_3)/8} \approx 1086$$

PAPI counters



Aggregate performance $N_e=1024$



Conclusions

- Mixed mode in CASINO achieves speed up factors in the range of 1.5/4 for 2/4 OpenMP threads for models with 1000 electrons on XT4.
- Our analysis predicts that the same speed up factors extends up to 2000 electrons models on XT6 due to larger cache memory.
- We have found a memory bound kernel (\bar{D}) that need further study.
- What is cause of the large overheads?



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