Scaling hybrid coarray/MPI miniapps on Archer

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CGPACK - cellular automata microstructure simulation library: https://sourceforge.net/projects/cgpack

- Solidification, recrystallisation, and fracture of polycrystalline microstructures.
- Fortran 2008 coarrays + TS 18508 [1] extensions.
- HECToR, ARCHER, Intel, OpenCoarrays/GCC systems.
- BSD license



 $\{100\}$ and $\{110\}$ micro-cracks in individual crystals merge into a macro-crack.

CGPACK design

- CA space coarray - 4D array, 3D corank structured grid [2, 3, 4].
- Integer cell states
- Fixed or self-similar boundaries
- Traditional halo exchange



CGPACK space coarray: integer, allocatable :: space(:,:,:,:)[:,:,:]

- Discrete space, discrete time
- Mesh independent results require 2 10⁵ CA cells per crystal on average [5].
- Crystal (grain) is a cluster of cells of the same value.



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CGPACK IO - unresolved

- MPI/IO speeds up to 2.3GB/s on HECToR (Cray XE6) [6].
- MPI/IO can reach 14GB/s on ARCHER (Cray XC30)
 [7].

 NetCDF (not yet implemented) higher level of abstraction, sits on top of MPI/IO. [8].



 10^6 grains, 10^{11} cells – 400GB dataset, >4 hours on 1000 ARCHER nodes (24k cores).

CGPACK scaling

- Up to 32k cores on HECToR and ARCHER for solidification problems.
- Scaling varies for different programs built with CGPACK, depending on which routines are called, in what order and requirements for synchronisation.



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ParaFEM - scalable general purpose finite element library

http:// parafem. org.uk

- Fortran 90
 MPI
- Highly portable, many users
 [9]
- Excellent scaling
- BSD license





Cellular Automata Finite Element (CAFE)

- Used for solidification [10], recrystallisation [11] and fracture [12, 13].
- FE continuum mechanics - stress, strain, etc.
- CA crystals, crystal boundaries, cleavage, grain boundary fracture
- $FE \rightarrow CA$ stress, strain
- $CA \rightarrow FE$ damage variables



CAFE design: structured CA grid + unstructured FE grid



 $\mathsf{FE}\to\mathsf{CA}$ mapping via a private allocatable array of derived type:

type mcen						
integer :: image, elnum						
real :: centr(3)						
end type mcen						
type(mcen), allocatable	::	lcentr(:)				

based on coordinates of FE centroids calculated by each MPI process and stored in centroid_tmp coarray:

```
type rca
  real, allocatable :: r(:,:)
end type rca
type( rca ) :: centroid_tmp[*]
:
allocate( centroid_tmp%r(3, nels_pp) )
where nels_pp is the number of FE stored on this PE.
```

lcentr arrays on images P and Q



E 990

All-to-all vs nearest neighbour for lcentr

cgca_pfem_cenc - all-to-all routine.

cgca_pfem_map - nearest neighbour - temporary arrays and coarray collectives CO_SUM and CO_MAX, described in TS 18508 [1] and will be included in the next revision of the Fortran standard, Fortran 2015. At the time of writing coarray collectives are available on Cray systems as extension to the standard [14]. The two routines differ in their use of remote communications.

cgca_pfem_map

integer :: maxfe, start, pend, ctmpsize real, allocatable :: tmp(:,:) ! Calc. the max num. of FE stored on this img $maxfe = size(centroid_tmp\%r, dim=2)$ ctmpsize = maxfe call co_max(source = maxfe)} allocate(tmp(maxfe*num_images(),5), source=0.0) ! Each image writes to a unique portion of tmp start = $(this_image() - 1)*maxfe + 1$ pend = start + ctmpsize - 1 tmp(start:pend,1)=real(this_image(),kind=4) ! Write element number *as real* tmp(start : pend, 2) = & real ((/(j, j = 1, ctmpsize)), kind=4)! Write centroid coord tmp(start : pend, 3:5) = &transpose(centroid_tmp%r(:,:)) $call co_sum(source = tmp)$

Initial CAFE scaling





Profiling function distribution for ParaFEM/CGPACK MPI/coarray miniapp with all-to-all routine cgca_gcupda at 7200 cores.

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Initial profiling

```
100.0% | 20,520.4 | -- | -- |Total
  71.4% | 14.649.9 | -- | -- | USER
                                     - - - - - - - - - - - - - - - -
  38.7% | 7.950.6 | 913.4 | 10.3% |cgca gcupda$cgca m3clvg
|| 24.1% | 4,951.2 | 940.8 | 16.0% |cgca clvgp$cgca m3clvg
|| 3.1% | 638.0 | 70.0 | 9.9% |cgca pfem cenc$cgca m3pfem
|| 1.8% | 367.5 | 578.5 | 61.2% |cgca_hxi$cgca_m2hx_
11
    1.7% | 346.0 | 196.0 | 36.2% |cgca clvgn$cgca m3clvg
                                  _____
  19.8% 4.061.4 -- -- MPI
6.9% | 1,413.5 | 356.5 | 20.1% |mpi bcast
  5.4% | 1,098.3 | 419.7 | 27.7% |MPI BARRIER
3.3% | 670.0 | 322.0 | 32.5% |mpi recv
11
    3.0% | 615.3 | 61.7 | 9.1% |MPI ALLREDUCE
                                _____
   8.8% | 1.797.2 | -- | -- | ETC
    4.6% | 950.5 | 5.5 | 0.6% | DEALLOCATE
11
    3.2% | 654.2 | 110.8 | 14.5% |gotoblas dgemy n sandybridge
```

Raw profiling data for ParaFEM/CGPACK MPI/coarray miniapp with all-to-all routine cgca_gcupda at 7200 cores.

cgca_gcupda - all-to-all

```
integer :: gcupd(100,3)[*], rndint, j, &
          img, gcupd_local(100,3)
real :: rnd
call random_number( rnd )
rndint = int(rnd*num_images()) + 1
do i = rndint, rndint + num_images() - 1
img = i
if (img .gt. num_images()) &
      img = img - num_images()
  if (img .eq. this_image()) cycle
  gcupd_local(:,:) = gcupd(:,:)[img]
end do
```

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cgca_gcupdn - nearest neighbour

```
do i = -1 , 1
do i = -1 , 1
do k = -1 , 1
 ! Get the coindex set of the neighbour
 ncod = mycod + (/ i, j, k /)
 gcupd_local(:,:) = \&
    gcupd (:,:)[ncod (1), ncod (2), ncod (3)]
end do
end do
end do
```

Note: the nearest neighbour must be called *multiple times* to propagate changes from every image to all other images.

Profiling cgca_gcupdn



Profiling function distribution for ParaFEM/CGPACK MPI/coarray miniapp with the neareast neighbour routine cgca_gcupdn at 7200 cores.

Profiling cgca_gcupdn

```
100.0% | 12.199.5 | -- | -- |Total
 44.8% 5.459.7 -- USER
  28.6% | 3.484.0 | 582.0 | 14.3% |cgca clvgp$cgca m3clvg
1 5.5% 666.1 93.9 12.4% cgca_pfem_cenc$cgca_m3pfem_
|| 3.2% | 393.1 | 752.9 | 65.7% |cgca_hxi$cgca_m2hx_
11
 2.8% | 346.0 | 176.0 | 33.7% |cgca_clvgn$cgca_m3clvg_
|| 1.4% | 165.2 | 37.8 | 18.6% |cgca_sld$cgca_m3sld_
|| 1.0% | 126.0 | 82.0 | 39.4% |xx14
 36.7% | 4,472.1 | -- | -- | MPI
  12.2% | 1,484.4 | 380.6 | 20.4% |mpi bcast
|| 10.6% | 1,287.9 | 389.1 | 23.2% |MPI BARRIER
|| 5.9% | 714.9 | 90.1 | 11.2% |MPI ALLREDUCE
|| 5.7% | 689.4 | 338.6 | 32.9% |mpi recv
H.
  1.5% | 179.1 | 417.9 | 70.0% |MPI REDUCE
  18.5% 2,256.1 -- ETC
|| 12.1% | 1,480.9 | 4.1 | 0.3% | DEALLOCATE
11
  5.4% 653.8 95.2 12.7% gotoblas dgemv n sandybridge
```

Raw profiling data for ParaFEM/CGPACK MPI/coarray miniapp with the neareast neighbour routine cgca_gcupdn at 7200 cores.

Scaling improvement with cgca_gcupdn over cgca_gcupda



Scaling limit increased from 2k to 7k cores.

Profiling with cgca_pfem_map



Profiling function distribution for ParaFEM/CGPACK MPI/coarray miniapp with cgca_gcupdn and cgca_pfem_map at 7200 cores.

Profiling with cgca_pfem_map

Table 1: Profile by Function Samp | Samp% | Imb. | Imb. |Group Samp Samp% | Function PE=HTDE Thread=HIDE 100.0% 9,903.4 -- - Total 43.6% 4.321.6 -- USER 31.4% | 3,110.7 | 589.3 | 15.9% |cgca_clvgp\$cgca_m3clvg_ Raw profiling data 3.5% | 346.0 | 513.0 | 59.7% |cgca hxi\$cgca m2hx 3.5% | 342.0 | 175.0 | 33.8% |cgca clvgn\$cgca m3clvg for ParaFEM/CG-1.2% | 116.3 | 4.7 | 3.9% |cgca_pfem_map\$cgca_m3pfem_ PACK MPI/coarray 11 1.1% | 106.8 | 1,537.2 | 93.5% |cgca_clvgsd\$cgca_m3clvg_ 24.1 | 19.5% |cgca sld\$cgca m3sld 1.0% 99.9 miniapp with 38.4% 3.803.6 -- - MPI cgca_gcupdn and cgca_pfem_map at 14.6% | 1,446.6 | 350.4 | 19.5% |mpi_bcast 9.4% | 932.4 | 473.6 | 33.7% |MPI_BARRIER 7200 cores. Ш 7.0% | 689.5 | 371.5 | 35.0% |mpi recv 4.9% | 489.3 | 76.7 | 13.6% |MPI ALLREDUCE 1.5% | 145.4 | 314.6 | 68.4% |MPI REDUCE 17.8% | 1.766.8 | -- | -- |ETC 9.9% 983.9 8.1 0.8% DEALLOCATE 6.6% 652.3 93.7 | 12.6% |gotoblas dgemv n sandybridge

Profiling with cgca_pfem_map



obtained, only from about 1000 cores. $\langle - \rangle \langle - \rangle \langle - \rangle \langle - \rangle \rangle \langle - \rangle$

Issues with CrayPAT

cgca_gcupda is top in sampling results, but is absent from tracing. It is called the same number of times as cgca_hxi.

	29.7%	99.743118		5,226,813.1 USER
П	17.4%	58.326659	36.082315 38.2%	5.0 cgca_clvgp\$cgca_m3clvg_
	5.6%	18.876152	5.062089 21.1%	<pre>1.0 cgca_pfem_cenc\$cgca_m3pfem_</pre>
	3.3%	11.145318	15.328335 57.9%	1.0 xx14_
П	1.7%	5.705317	8.788733 60.6%	5,224,771.1 cgca_clvgn\$cgca_m3clvg_
	1.7%	5.689672	1.910819 25.1%	2,035.0 cgca_hxi\$cgca_m2hx_
11				

Issues with CrayPAT

All profiling was done with single thread.

```
CrayPat/X: Version 6.2.2 Revision 13378 (xf 13240) 11/20/14 14:32:58
Number of PEs (MPI ranks): 480
```

Numbers of PEs per Node: 24 PEs on each of 20 Nodes

Numbers of Threads per PE: 3

Number of Cores per Socket: 12 Execution start time: Thu Mar 3 13:40:17 2016 System name and speed: tdsmom 2701 MHz

Incorrect number of threads indentified by CrayPAT in a tracing experiment of ParaFEM/CGPACK MPI/coarray miniapp with cgca_gcupda.

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Future work - optimisation of coarray synchronisation



- Some routines have sync inside.
- Other sync responsibility is left to the end user.
- Over-synchronisation?
- Enough sync is required by the standard. A standard conforming Fortran coarray program will not deadlock or suffer races.

ISO/IEC JTC1/SC22/WG5 N2074, TS 18508 Additional Parallel Features in Fortran, 2015.



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